Maximum Persistency via Iterative Relaxed Inference with Graphical Models

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Figure 1: Progress of partial optimality methods. Top line corresponds to a stereo model with Potts interactions and large aggregating windows for unary costs used in [2, 5] (instance published by [2]). Bottom line is a more refined stereo model with truncated linear terms [8] (instance in [1]). Hashed area indicates that the optimal persistent label in the pixel is not found (but some non-optimal labels might have been eliminated). Solution completeness is given by the percent of persistent labels. Graph cut based methods are fast but only efficient for strong unary terms. LP-based methods are able to determine a larger persistent assignments but are extremely slow, prior to this work. Note, our method is set up to determine strong persistency, a partial assignment that holds for all optimal solutions, while other methods here find a part of any optimal solution.

We consider the NP-hard problem of MAP-inference for graphical mod- Properties when subproblems are solved with TRW-S: els. We propose a polynomial time practically efficient algorithm for finding a part of its optimal solution. Specifically, our algorithm marks each label in each node of the considered graphical model either as (i) optimal, meaning that it belongs to all optimal solutions of the inference problem; (ii) nonoptimal if it provably does not belong to any solution; or (iii) undefined, which means our algorithm can not make a decision regarding the label. The labels that we proved optimal or non-optimal are called *persistent*.

Key ideas:

- We build on the Maximum Persistency [6] framework, which proved that most of the existing methods for partial optimality can be explained by a simple local domination condition if only one supplies the right reparametrization of the energy function.
- Finding the maximum subset of persistent labels can be formu-• lated [6] as a big linear program that optimizes over reparametrizations and a subset of labels deemed persistent at the same time. It is a challenging problem and large scale instances can only be addressed by a windowing technique [6] – a semi-local condition.
- We solve the same maximum persistency problem instead by iteratively solving standard LP relaxation for a series of auxiliary energy problems, similarly to the approach in [7]. We thus unite [6] and [7].

Key features of our approach:

- Invariant to reparametrization and order of labels.
- · Fast approximate dual solvers can be employed without compromising correctness and global persistency guarantees.
- Requires an approximate solution to LP relaxation as a starting point.
- Can be viewed as making an approximate solver for LP-relaxation to be able to prove optimality of a part of its solution.

More specifically, we demonstrated our approach using TRW-S [4] for solving auxiliary subproblems.

- Closely approximates maximum persistency LP (evaluated on small random problems).
- Fast message passing transfers to auxiliary problems.
- The method is correct using a finite number of TRW-S iterations.
- Subproblems can be solved incrementally, reusing the messages.
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This is an extended abstract. The full paper is available at the Computer Vision Foundation webpage.