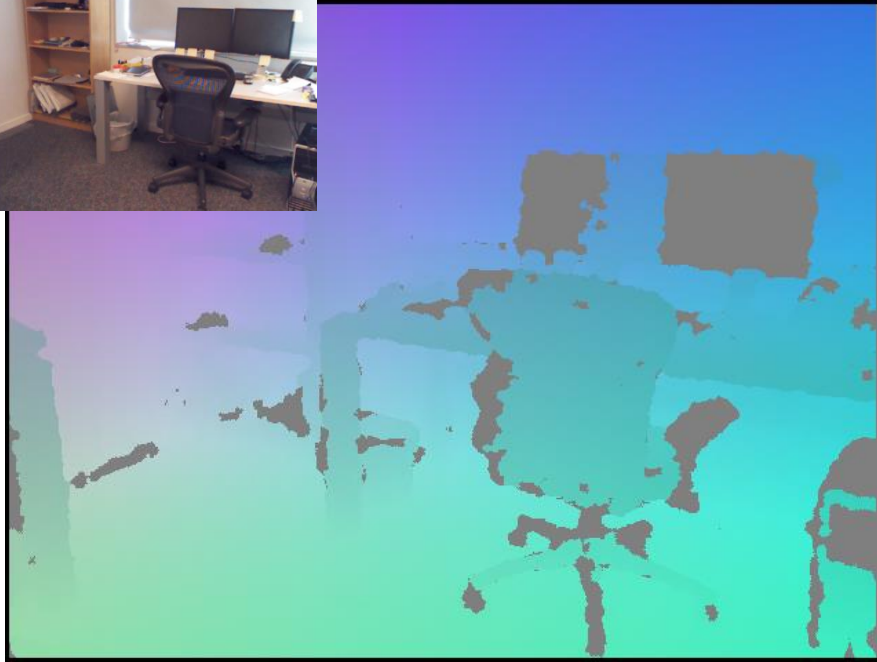
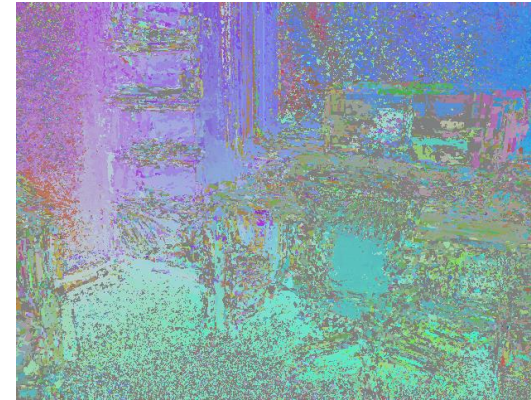


Object Coordinate Regression Results

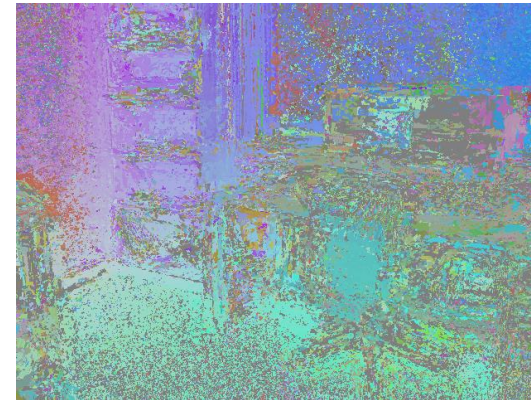


X^{Obj} (ground truth)

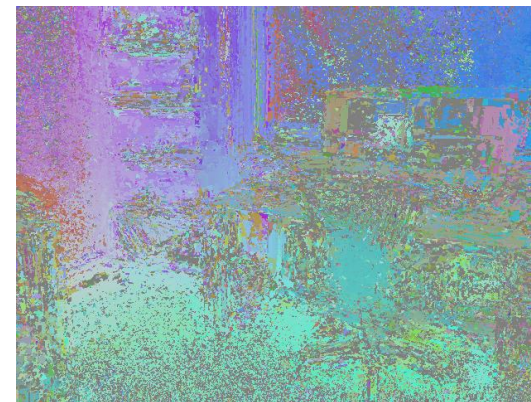
Problem: Outliers
Solution: RANSAC



X^{Obj} (tree 1)



X^{Obj} (tree 2)



X^{Obj} (tree 3)

RANSAC

```
1:   $\mathbf{R}^*, \mathbf{C}^*$ 
2:   $E^* := 0$ 
3:  repeat  $n$  times:
4:    sample  $\{(\mathbf{X}_1^{Cam}, \mathbf{X}_1^{Obj}), (\mathbf{X}_2^{Cam}, \mathbf{X}_2^{Obj}), (\mathbf{X}_3^{Cam}, \mathbf{X}_3^{Obj})\}$ 
5:     $\mathbf{R}, \mathbf{C} :=$  solve Kabsch
6:     $E(\mathbf{R}, \mathbf{C}) := \sum_{i \in I} \sum_{t \in T} \mathbb{1}[\|\mathbf{X}_i^{Cam} - (\mathbf{R}\mathbf{X}_{i,t}^{Obj} - \mathbf{C})\| < \tau]$ 
7:    if  $E(\mathbf{R}, \mathbf{C}) > E^*$ :
8:       $E^* := E(\mathbf{R}, \mathbf{C})$ 
9:       $\mathbf{R}^* := \mathbf{R}, \mathbf{C}^* := \mathbf{C}$ 
10: refine  $\mathbf{R}^*, \mathbf{C}^*$ 
```

E	... inlier count
τ	... inlier threshold
I	... set of image pixels
T	... set of regression trees

RANSAC

Input:



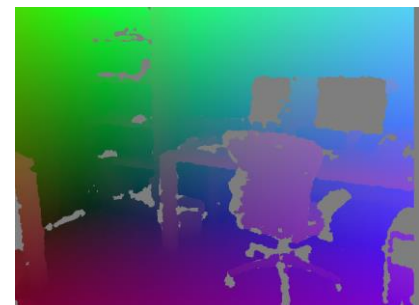
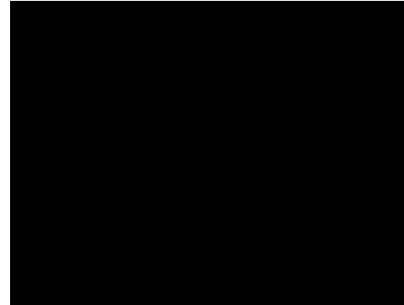
RGB-D

Forest Prediction:

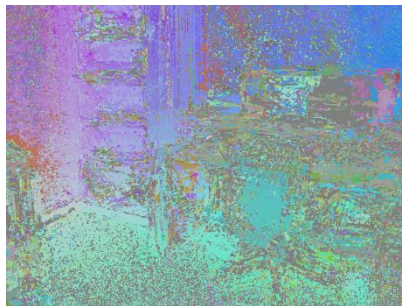


X^{Obj} (tree 1)

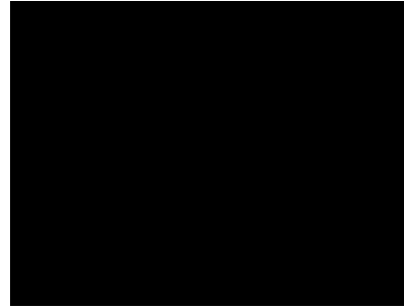
Inliers:



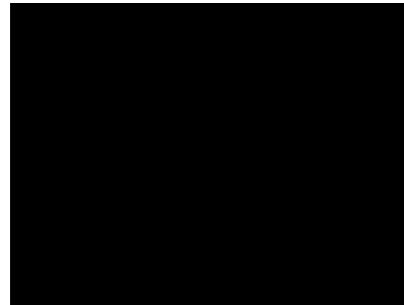
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



R^*, C^*

$E^* = 0$

repeat 3 times:

sample

$R, C := \text{Kabsch}$

$E(R, C) = ?$

if $E(R, C) > E^*$:

$E^* := E(R, C)$

$R^* := R, C^* := C$

refine R^*, C^*

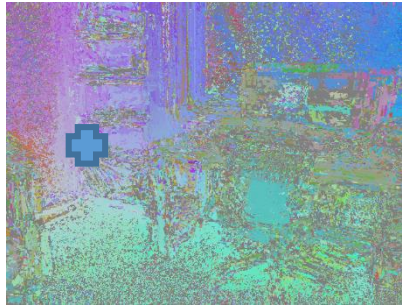
RANSAC

Input:



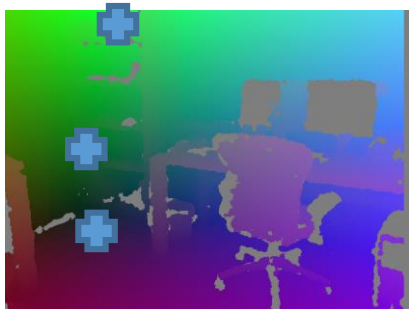
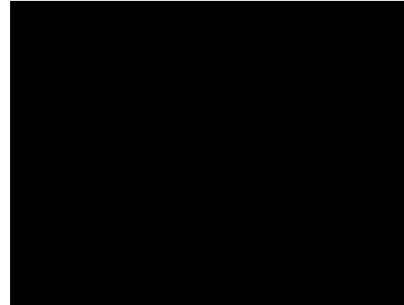
RGB-D

Forest Prediction:

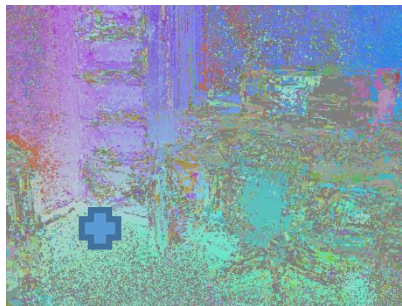


X^{Obj} (tree 1)

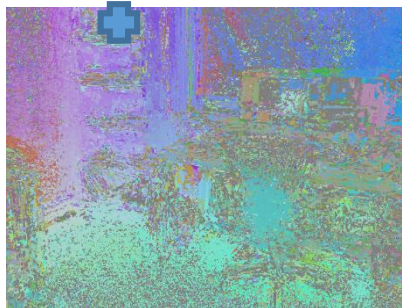
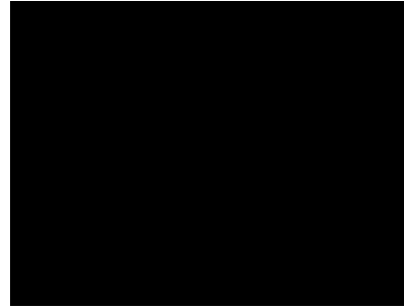
Inliers:



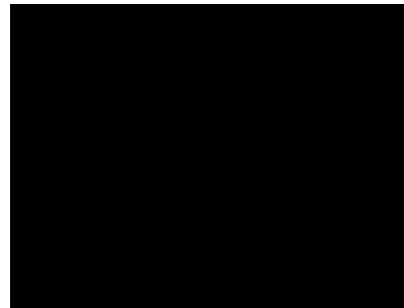
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



R^*, C^*

$E^* = 0$

repeat 3 times:

sample

$R, C := \text{Kabsch}$

$E(R, C) = ?$

if $E(R, C) > E^*$:

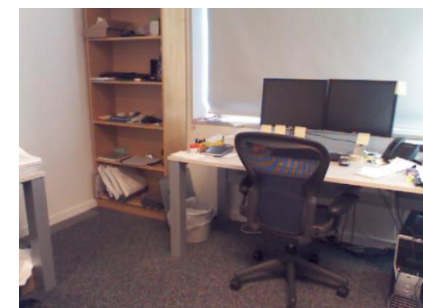
$E^* := E(R, C)$

$R^* := R, C^* := C$

refine R^*, C^*

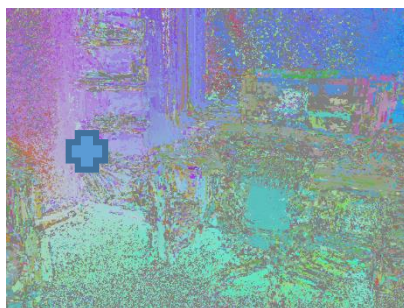
RANSAC

Input:



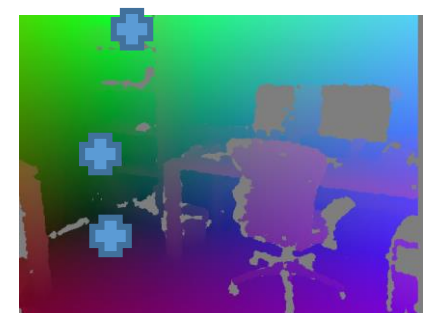
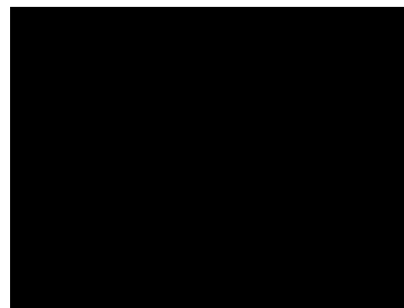
RGB-D

Forest Prediction:

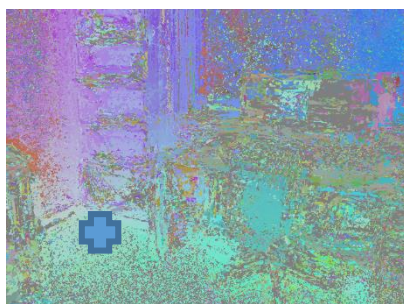


X^{Obj} (tree 1)

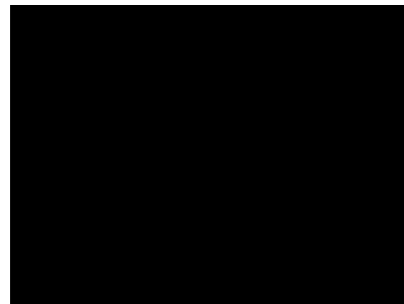
Inliers:



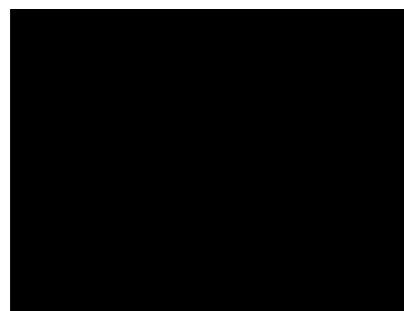
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



R^*, C^*

$E^* = 0$

repeat 3 times:

sample

$R_1, C_1 := \text{Kabsch}$

$E(R, C) = ?$

if $E(R, C) > E^*$:

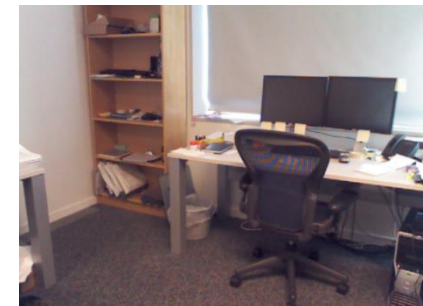
$E^* := E(R, C)$

$R^* := R, C^* := C$

refine R^*, C^*

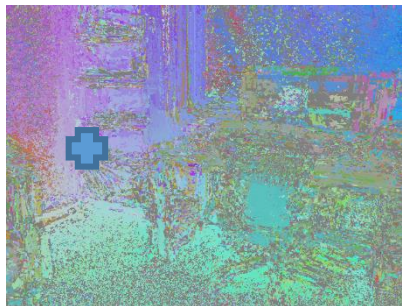
RANSAC

Input:



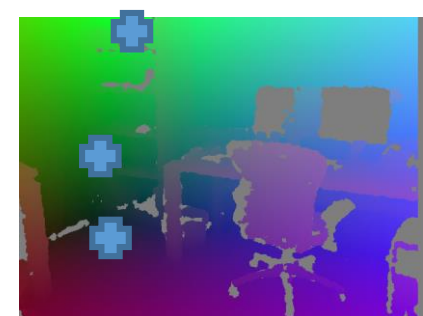
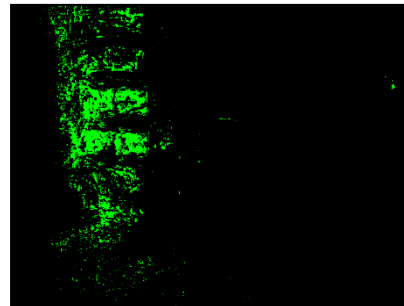
RGB-D

Forest Prediction:

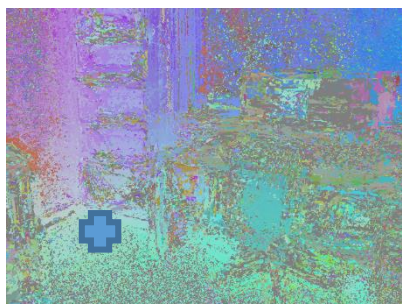


X^{Obj} (tree 1)

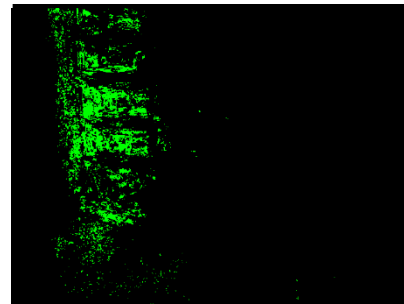
Inliers:



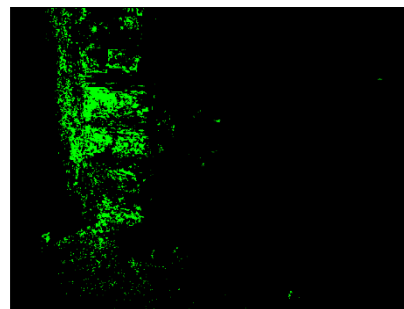
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



R^*, C^*

$E^* = 0$

repeat 3 times:

sample

$R_1, C_1 := \text{Kabsch}$

$E(R_1, C_1) = 40772$

if $E(R, C) > E^*$:

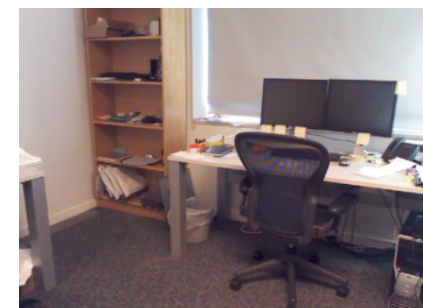
$E^* := E(R, C)$

$R^* := R, C^* := C$

refine R^*, C^*

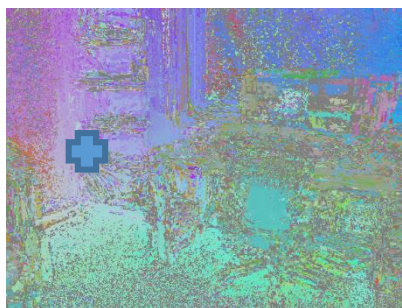
RANSAC

Input:



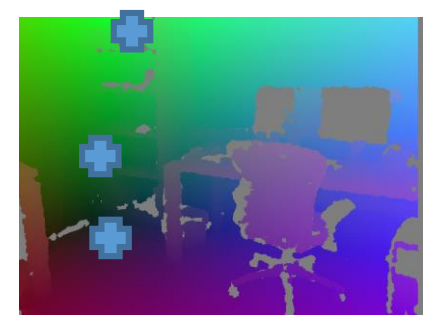
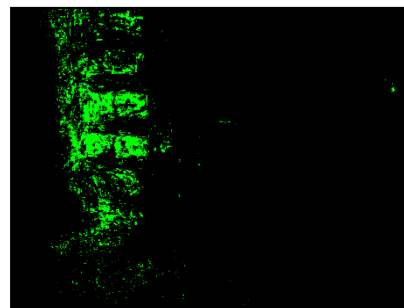
RGB-D

Forest Prediction:

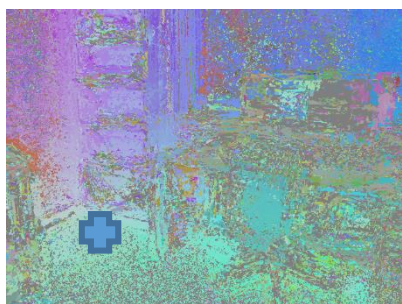


X^{Obj} (tree 1)

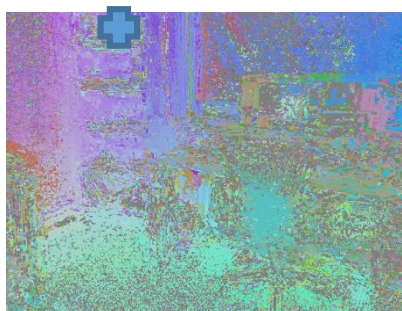
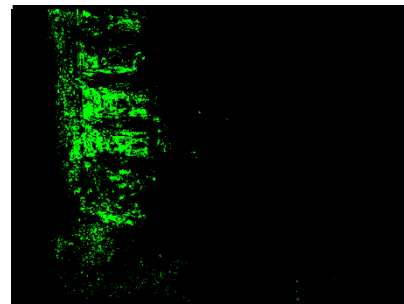
Inliers:



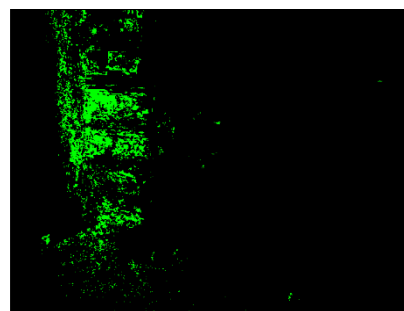
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



R^*, C^*

$E^* = 0$

repeat 3 times:

sample

$R_1, C_1 := \text{Kabsch}$

$E(R_1, C_1) = 40772$

if $E(R_1, C_1) > E^*$:

$E^* := E(R_1, C_1)$

$R^* := R_1, C^* := C_1$

refine R^*, C^*

RANSAC

Input:



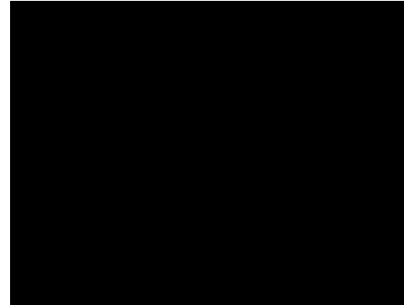
RGB-D

Forest Prediction:



X^{Obj} (tree 1)

Inliers:



$$R^* = R_1, C^* = C_1$$

$$E^* = 40772$$

repeat 2 times:

sample

$$R, C := \text{Kabsch}$$

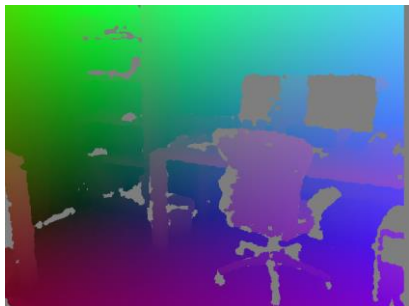
$$E(R, C) = ?$$

if $E(R, C) > E^*$:

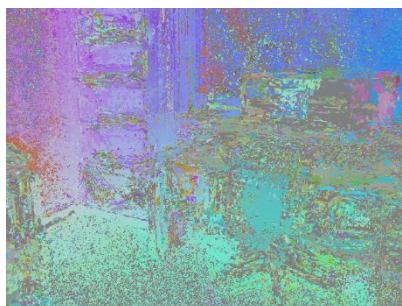
$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

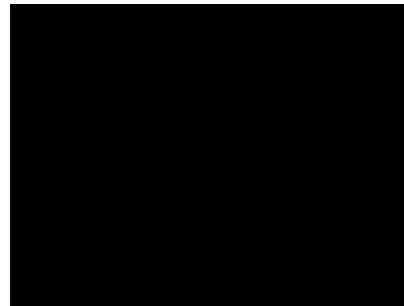
refine R^*, C^*



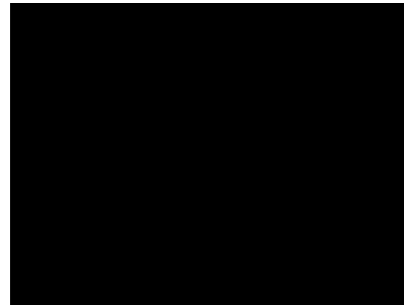
X^{Cam}



X^{Obj} (tree 2)

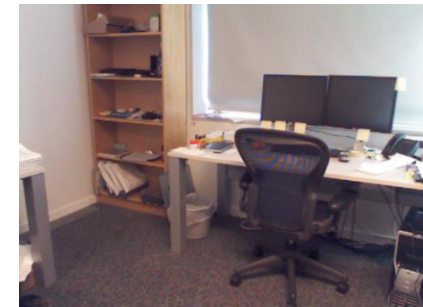


X^{Obj} (tree 3)



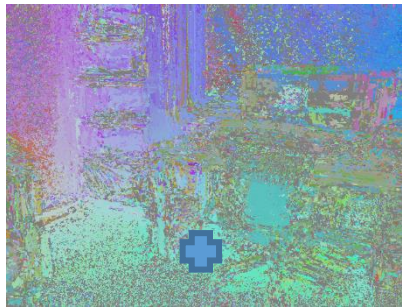
RANSAC

Input:



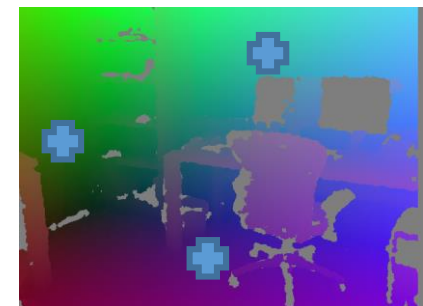
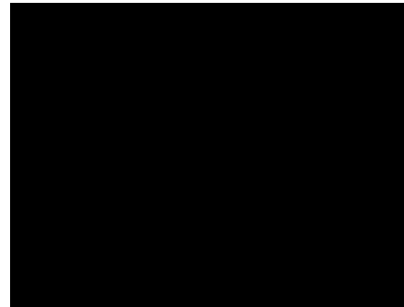
RGB-D

Forest Prediction:

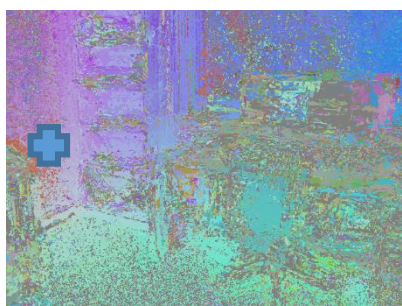


X^{Obj} (tree 1)

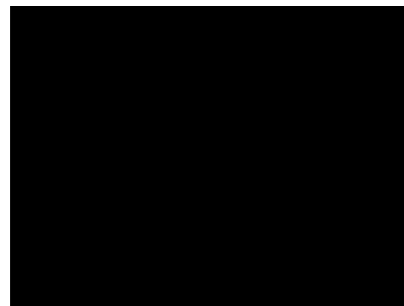
Inliers:



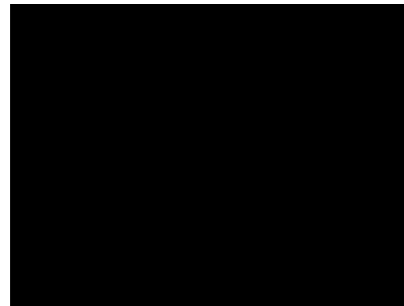
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_1, C^* = C_1$$

$$E^* = 40772$$

repeat 2 times:

sample

$$R, C := \text{Kabsch}$$

$$E(R, C) = ?$$

if $E(R, C) > E^*$:

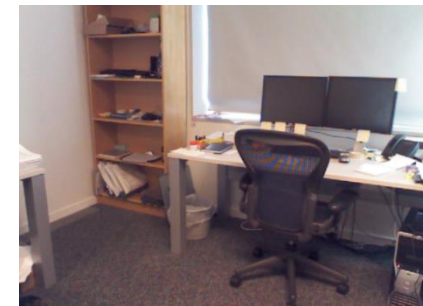
$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

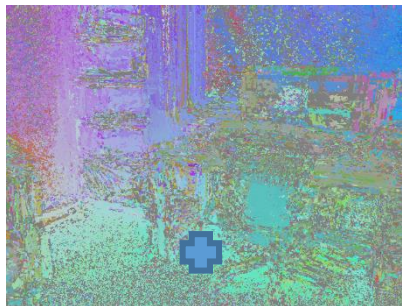
RANSAC

Input:



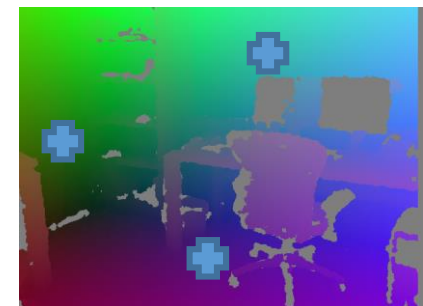
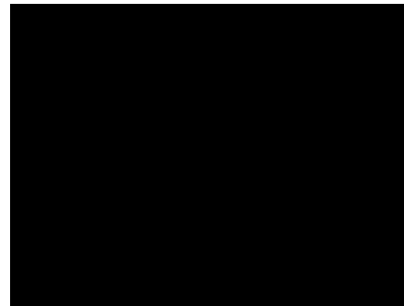
RGB-D

Forest Prediction:

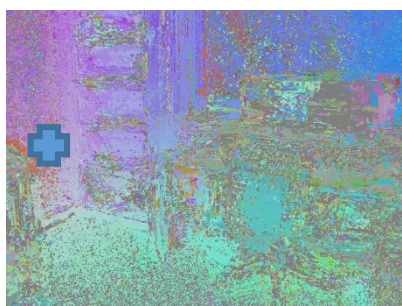


X^{Obj} (tree 1)

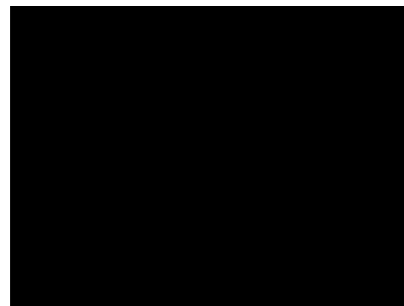
Inliers:



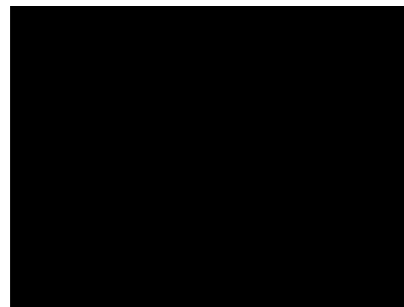
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_1, C^* = C_1$$

$$E^* = 40772$$

repeat 2 times:

sample

$$R_2, C_2 := \text{Kabsch}$$

$$E(R, C) = ?$$

if $E(R, C) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

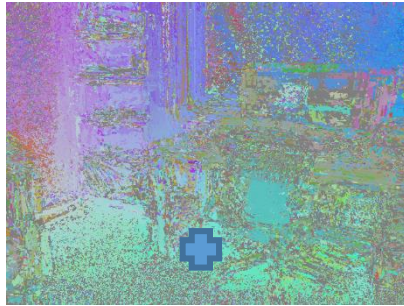
RANSAC

Input:



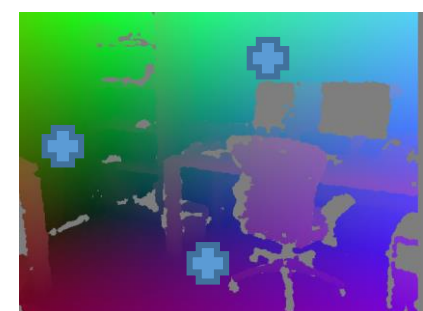
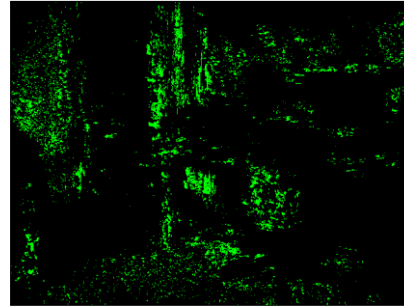
RGB-D

Forest Prediction:

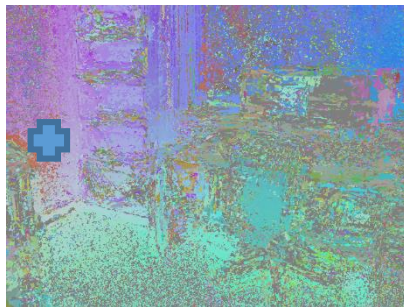


X^{Obj} (tree 1)

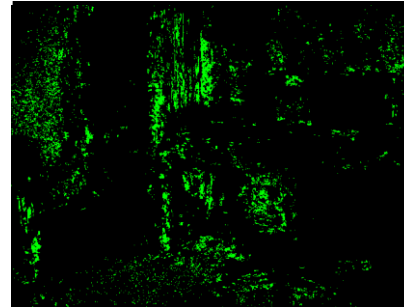
Inliers:



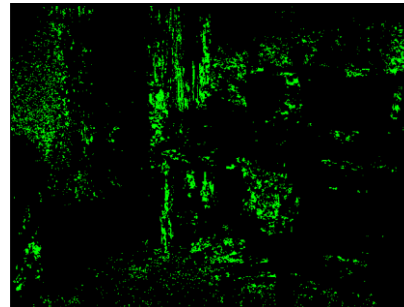
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_1, C^* = C_1$$

$$E^* = 40772$$

repeat 2 times:

sample

$$R_2, C_2 := \text{Kabsch}$$

$$E(R_2, C_2) = 54679$$

if $E(R, C) > E^*$:

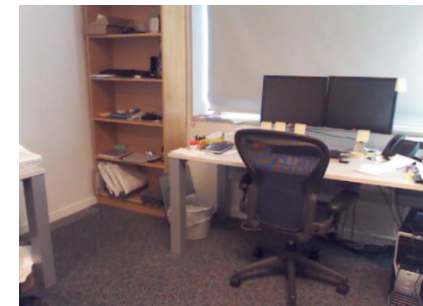
$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

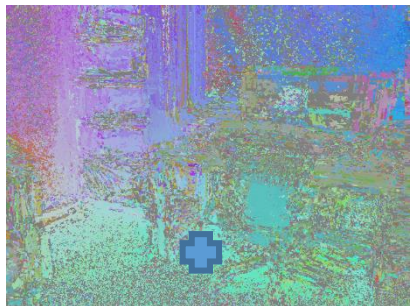
RANSAC

Input:



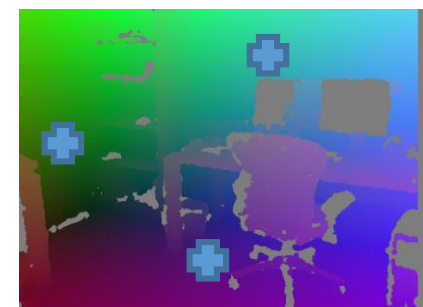
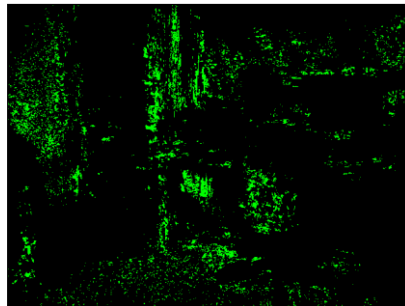
RGB-D

Forest Prediction:

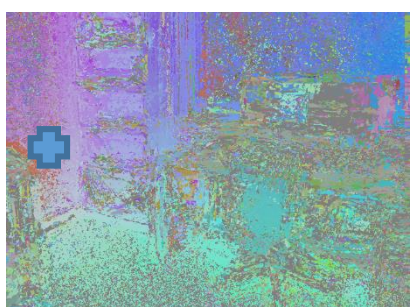


X^{Obj} (tree 1)

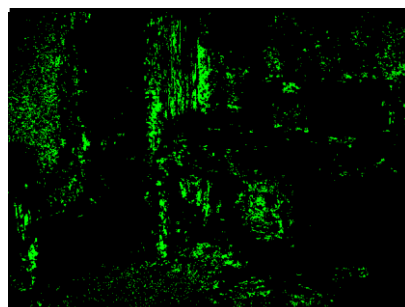
Inliers:



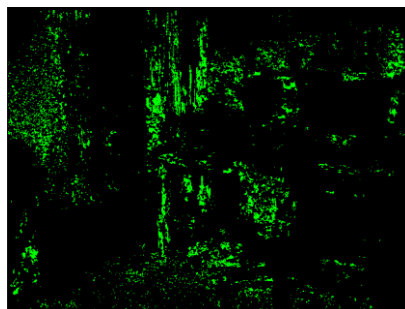
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_1, C^* = C_1$$

$$E^* = 40772$$

repeat 2 times:

sample

$$R_2, C_2 := \text{Kabsch}$$

$$E(R_2, C_2) = 54679$$

if $E(R_2, C_2) > E^*$:

$$E^* := E(R_2, C_2)$$

$$R^* := R_2, C^* := C_2$$

refine R^*, C^*

RANSAC

Input:



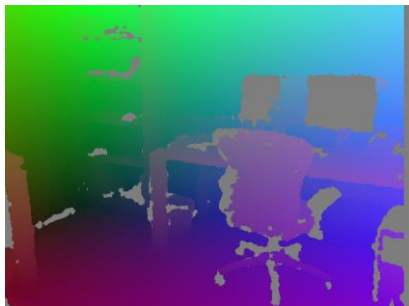
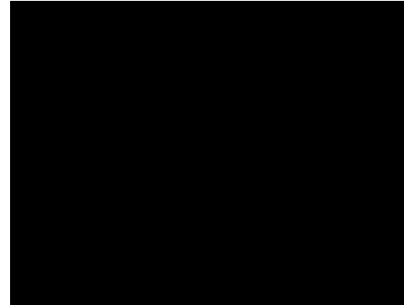
RGB-D

Forest Prediction:

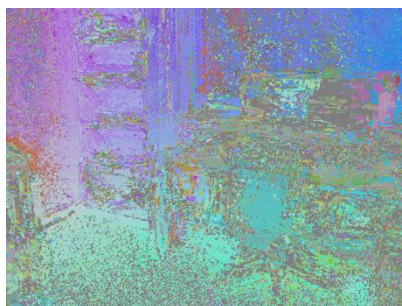


X^{Obj} (tree 1)

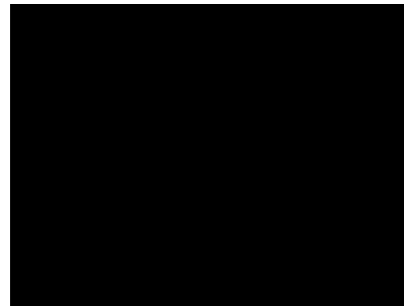
Inliers:



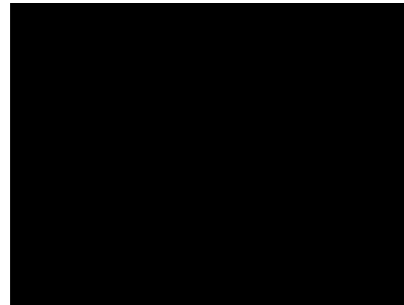
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_2, C^* = C_2$$

$$E^* = 54679$$

repeat 1 times:

sample

$$R, C := \text{Kabsch}$$

$$E(R, C) = ?$$

if $E(R, C) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

RANSAC

Input:



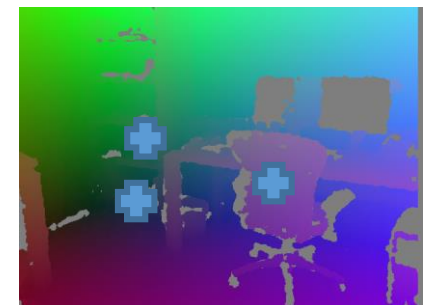
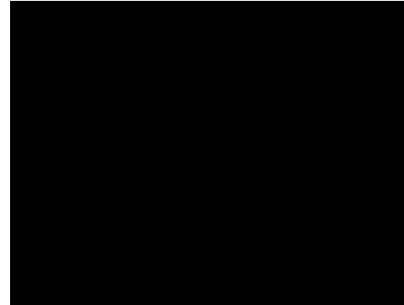
RGB-D

Forest Prediction:

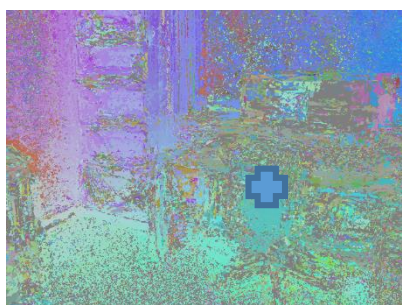


X^{Obj} (tree 1)

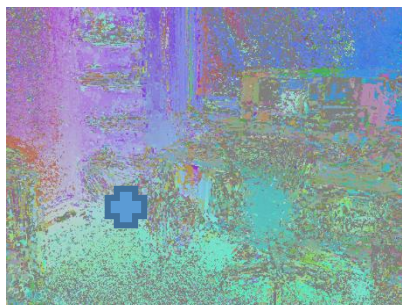
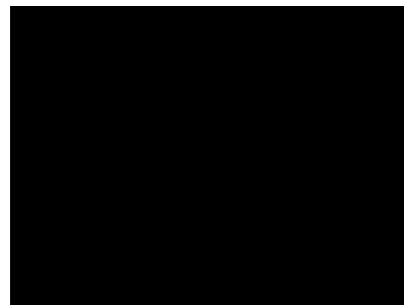
Inliers:



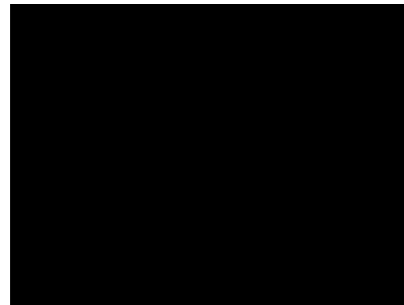
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



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$$E^* = 54679$$

repeat 1 times:

sample

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$$E(R, C) = ?$$

if $E(R, C) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

RANSAC

Input:



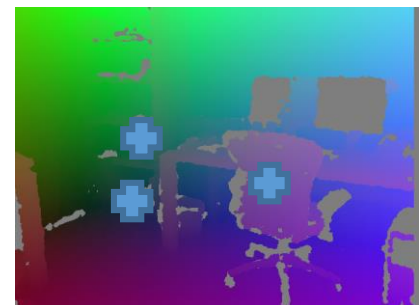
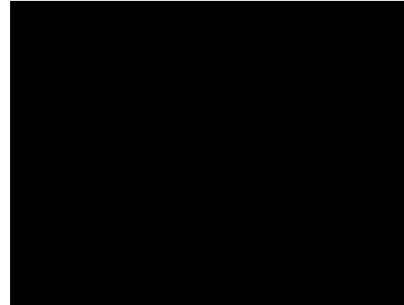
RGB-D

Forest Prediction:

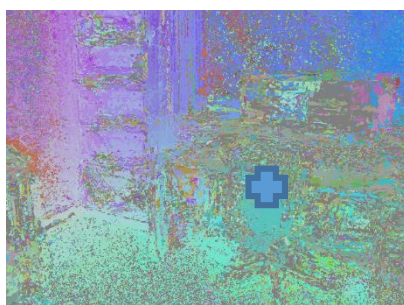


X^{Obj} (tree 1)

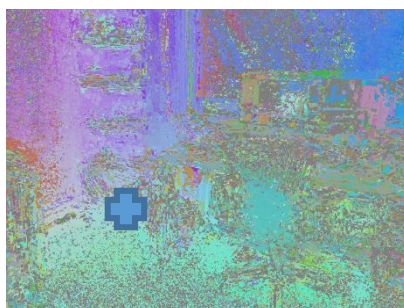
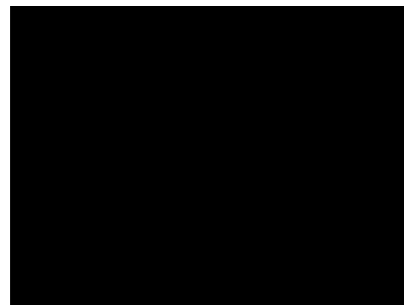
Inliers:



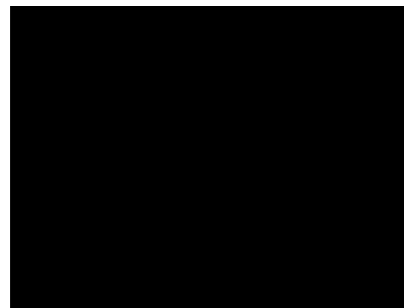
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_2, C^* = C_2$$

$$E^* = 54679$$

repeat 1 times:

sample

$$R_3, C_3 := \text{Kabsch}$$

$$E(R, C) = ?$$

if $E(R, C) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

RANSAC

Input:



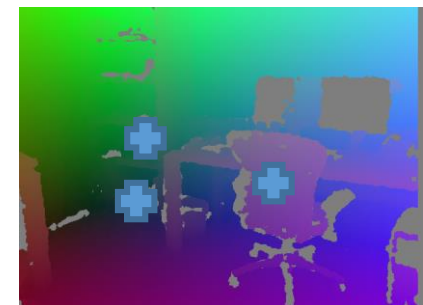
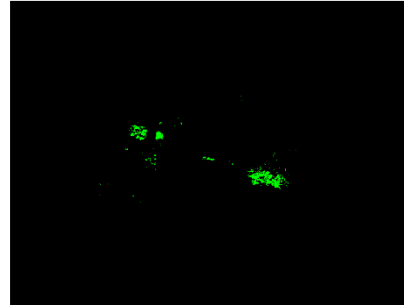
RGB-D

Forest Prediction:

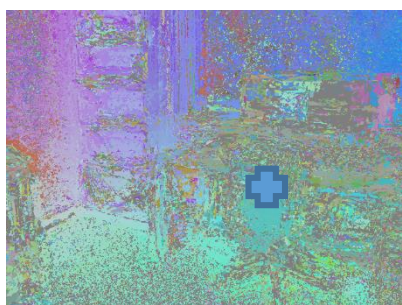


X^{Obj} (tree 1)

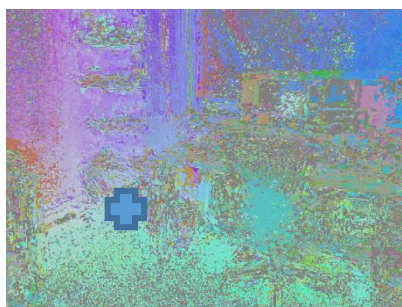
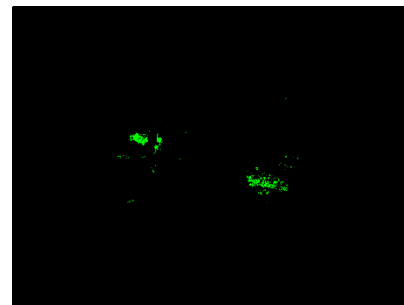
Inliers:



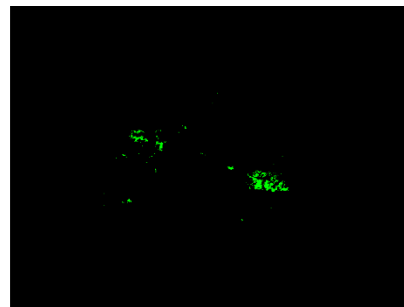
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_2, C^* = C_2$$

$$E^* = 54679$$

repeat 1 times:

sample

$$R_3, C_3 := \text{Kabsch}$$

$$E(R_3, C_3) = 3727$$

if $E(R, C) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

RANSAC

Input:



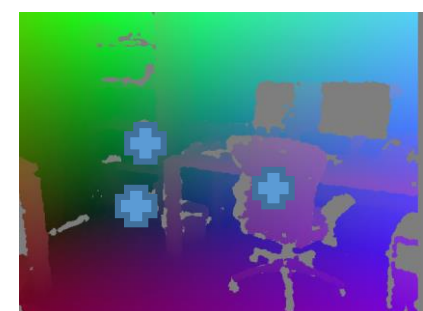
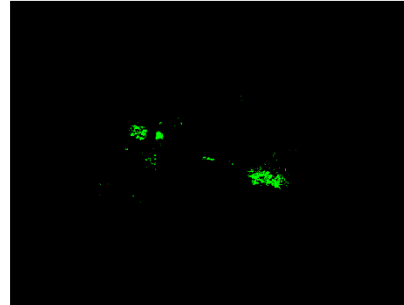
RGB-D

Forest Prediction:

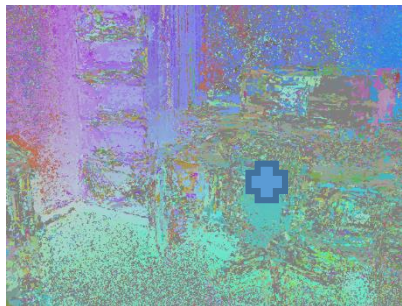


X^{Obj} (tree 1)

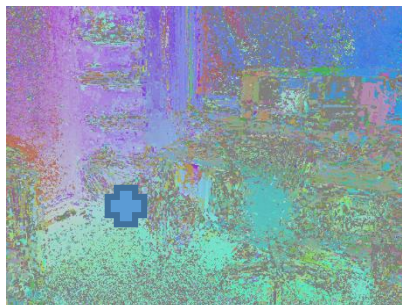
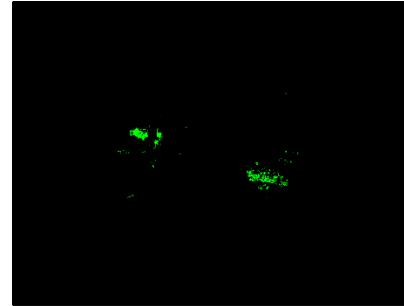
Inliers:



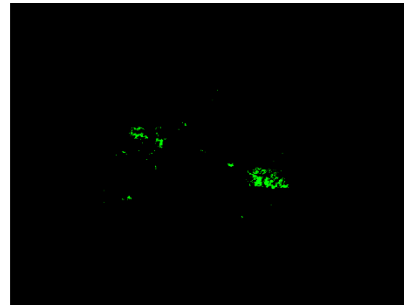
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_2, C^* = C_2$$

$$E^* = 54679$$

repeat 1 times:

sample

$$R_3, C_3 := \text{Kabsch}$$

$$E(R_3, C_3) = 3727$$

if $E(R_3, C_3) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

RANSAC

Input:



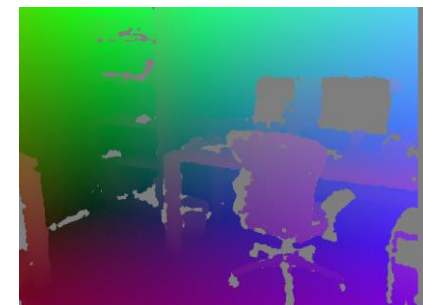
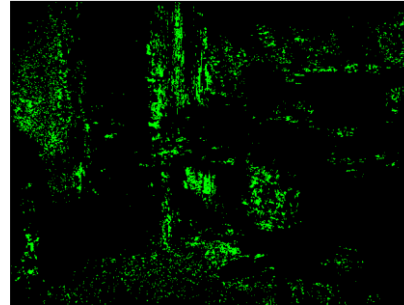
RGB-D

Forest Prediction:

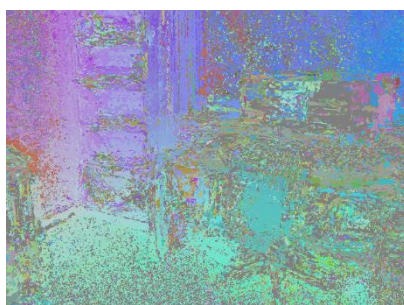


X^{Obj} (tree 1)

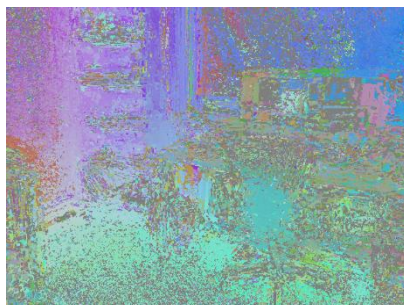
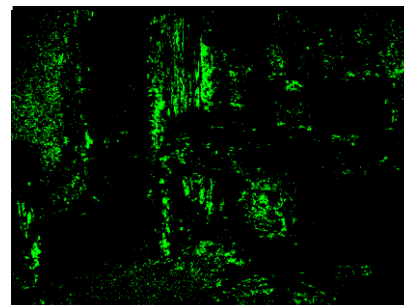
Inliers:



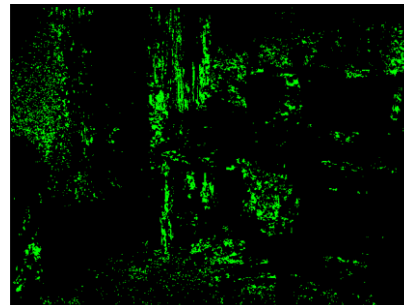
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_2, C^* = C_2$$

$$E^* = 54679$$

repeat 0 times:

sample

$$R, C := \text{Kabsch}$$

$$E(R, C) = ?$$

if $E(R, C) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

RANSAC

Input:



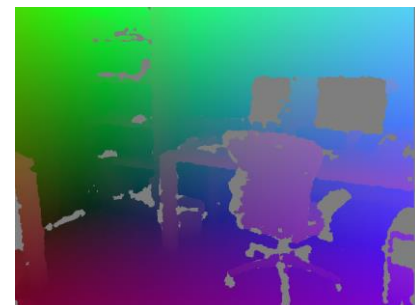
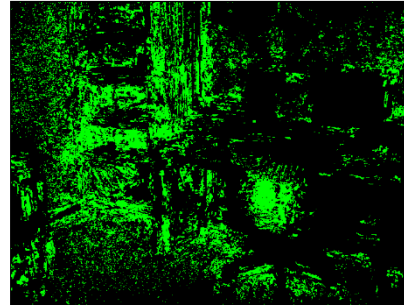
RGB-D

Forest Prediction:

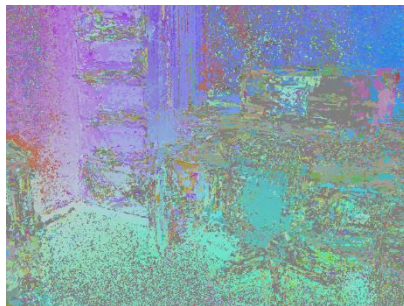


X^{Obj} (tree 1)

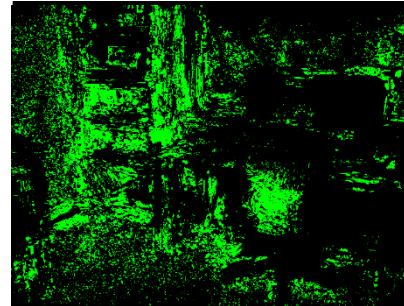
Inliers:



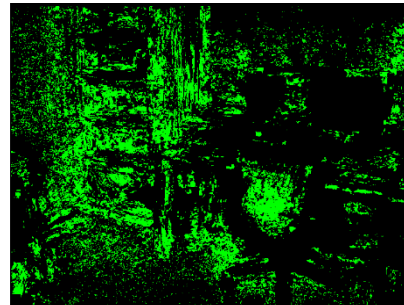
X^{Cam}



X^{Obj} (tree 2)



X^{Obj} (tree 3)



$$R^* = R_2, C^* = C_2$$

$$E^* = 54679$$

repeat 0 times:

sample

$$R, C := \text{Kabsch}$$

$$E(R, C) = ?$$

if $E(R, C) > E^*$:

$$E^* := E(R, C)$$

$$R^* := R, C^* := C$$

refine R^*, C^*

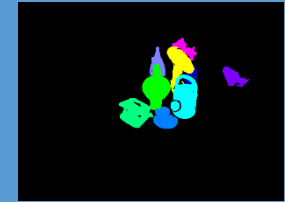
Final Inlier Count:

$$E(R^*, C^*) = 185414$$

Case Study: Pose Estimation and Pose Tracking

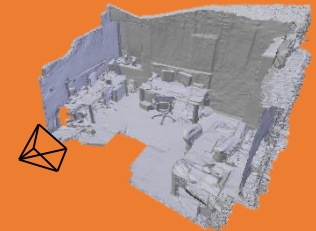
Image Segmentation:

- Decision Forest
- Features, Training Recap



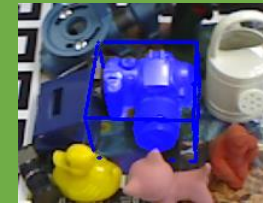
Camera Re-Localization:

- Regression Forest
- Split-Criteria, Kabsch, RANSAC



One-Shot Pose Estimation:

- Decision-Regression Forest
- Hypothesis Sampling, Hypotheses Energy



One-Shot Pose Estimation

Input: RGB-D image



Output: 6DoF Object Pose

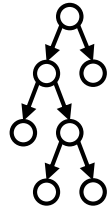


Dataset of Hinterstoisser et al., Model Based Training, Detection and Pose Estimation of Texture-Less 3D Objects in Heavily Cluttered Scenes, ACCV 12
Method of Brachmann et al., Learning 6d object pose estimation using 3d object coordinates, ECCV 14

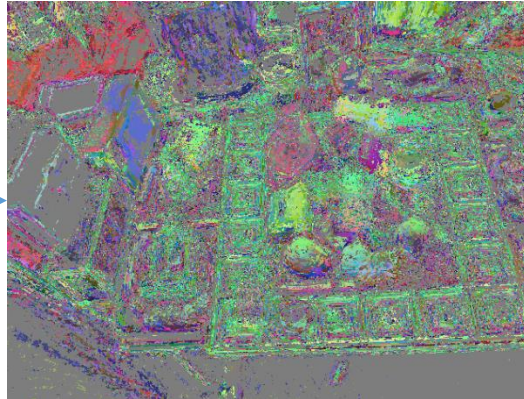
Why not use camera re-localization?

- $R_{Obj}(I_{3 \times 3} | - \tilde{t}_{Obj}) = (R_{Cam}(I_{3 \times 3} | - \tilde{C}_{Cam}))^{-1}$

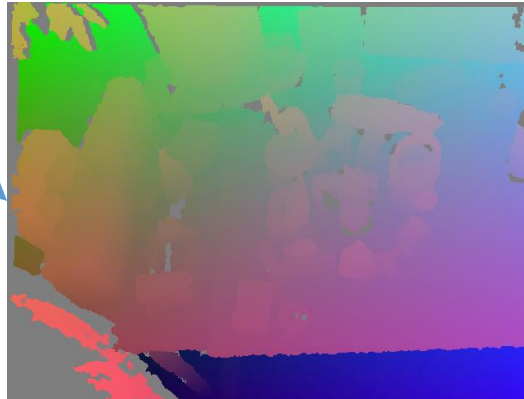
Input: RGB-D image



X^{Obj}



$K^{-1}x$



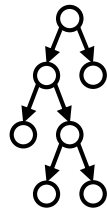
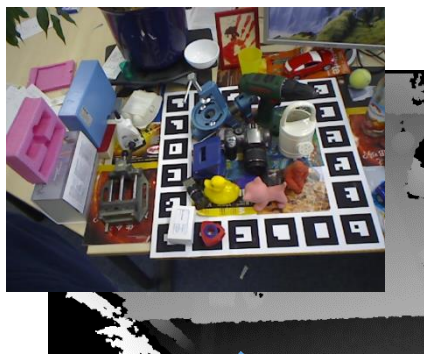
X^{Cam}

R ... rotation
 t, C ... translation
 K ... calibration matrix
 X ... 3D coordinate
 c ... object index
 $p(c)$... object probability

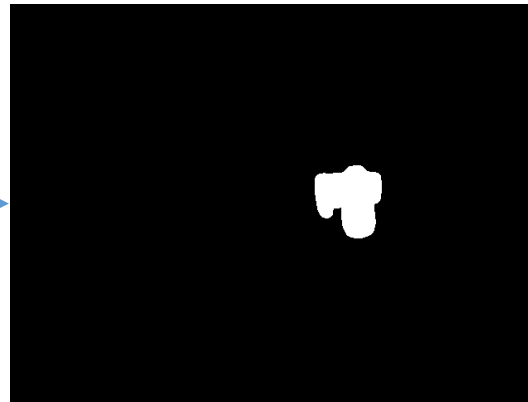
Why not use camera re-localization?

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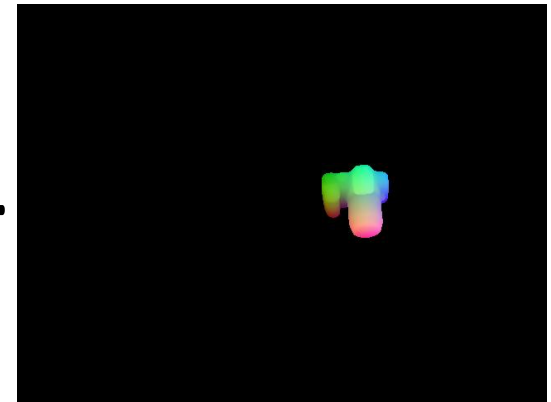
Input: RGB-D image



$p(c)$

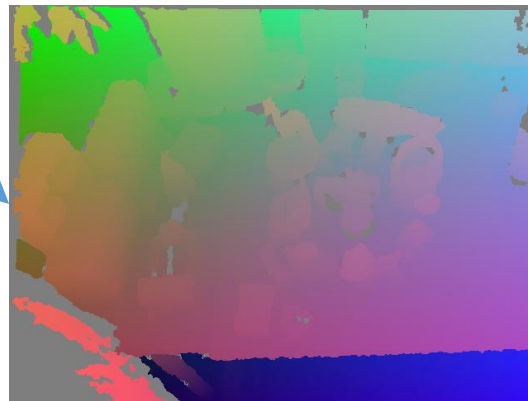


X^{Obj}



+

$K^{-1}x$



X^{Cam}

RANSAC



R ... rotation
 t, C ... translation
 K ... calibration matrix
 X ... 3D coordinate
 c ... object index
 $p(c)$... object probability

Regression-Decision Forest

- What has to be defined?
 - Features: Features: f^{DA-D} , f^{DA-RGB}
 - Split score: Proxy classes

Ape



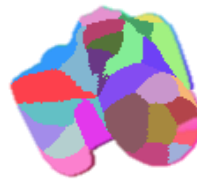
Class 1-125

Bench Vice



Class 126-250

Camera



Class 251-375

Can



Class 376-500

Background

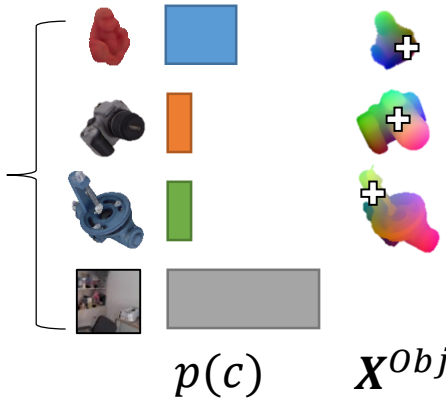
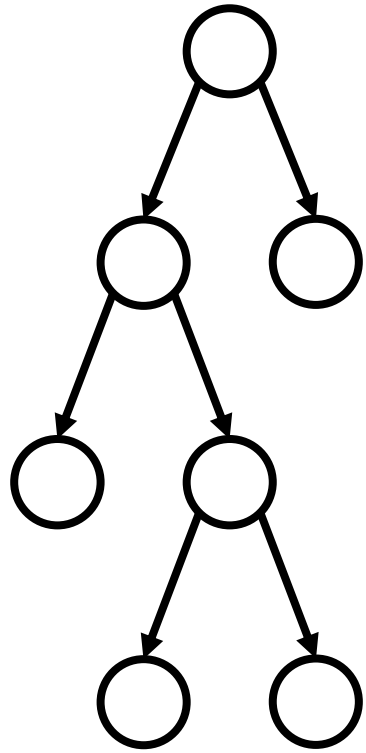


Class 0

- Stopping criterium: Max. tree depth
- Leaf distributions: ?

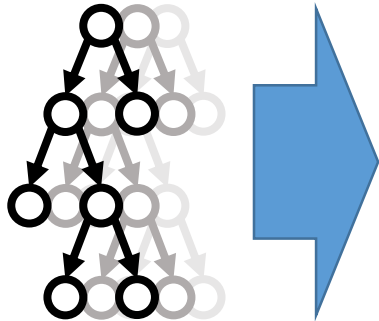
Leaf Distributions

- For each object:
 - Store object probability
 - Find modes
 - Store mean of largest mode



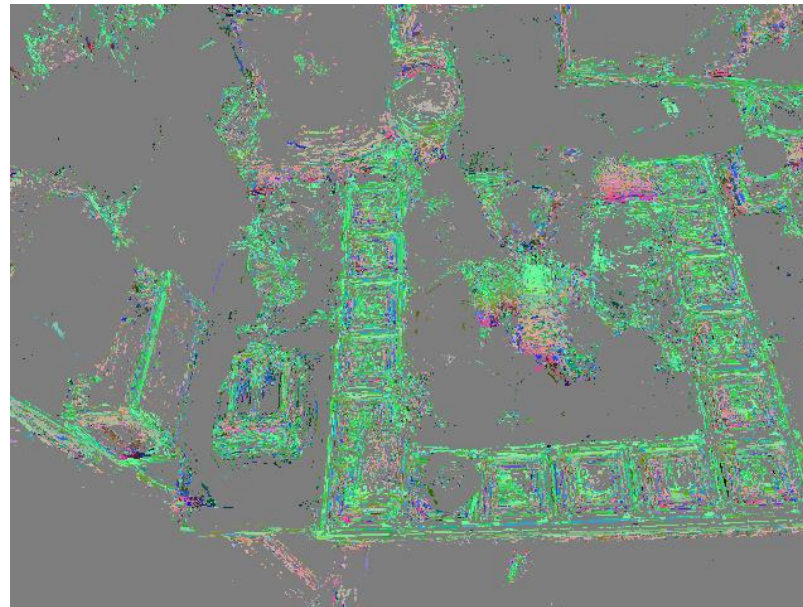
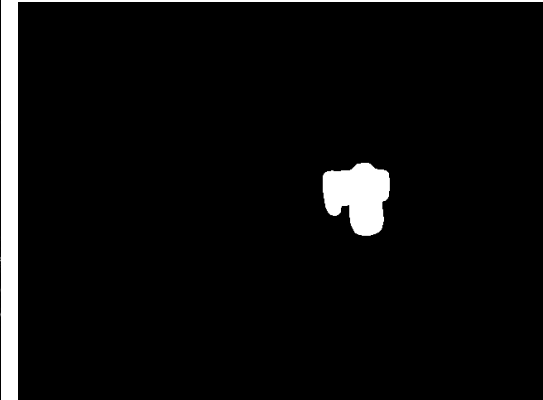
Formally: $p(X^{obj} | c)$

Forest Prediction

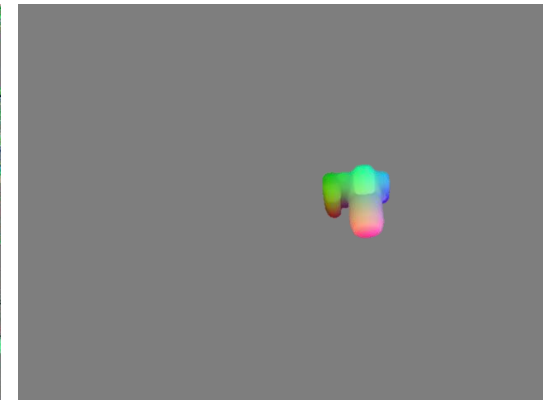


$p(c)$

Ground Truth



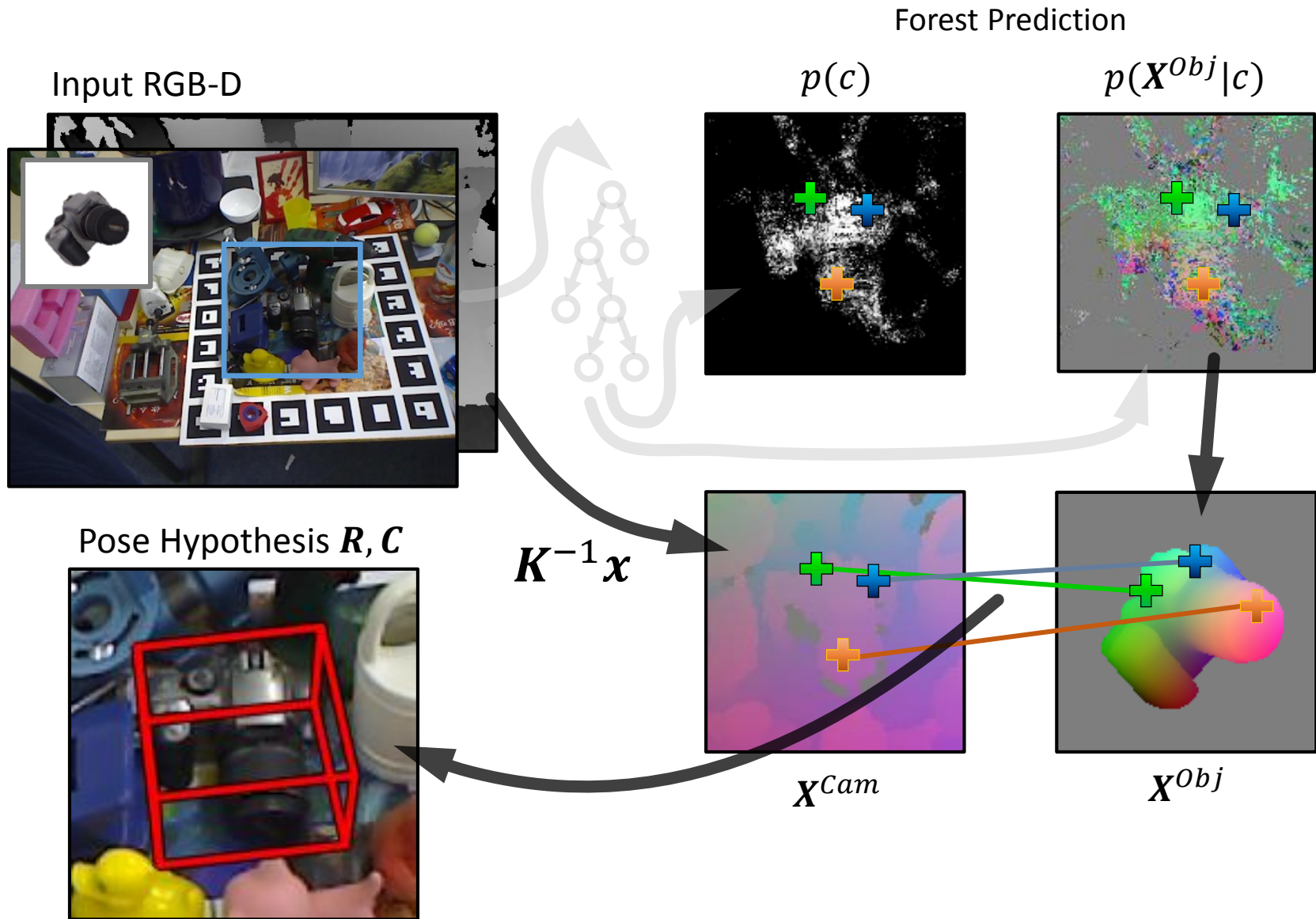
$p(X^{obj})$ (tree 1)




```
1:   $\mathbf{R}^*, \mathbf{C}^*$ 
2:   $E_c^* := 0$ 
3:  repeat  $n$  times:
4:      sample  $\{(\mathbf{X}_1^{Cam}, \mathbf{X}_1^{Obj}), (\mathbf{X}_2^{Cam}, \mathbf{X}_2^{Obj}), (\mathbf{X}_3^{Cam}, \mathbf{X}_3^{Obj})\}$ 
5:       $\mathbf{R}, \mathbf{C} :=$  solve Kabsch
6:      calculate  $E_c(\mathbf{R}, \mathbf{C})$ 
7:      if  $E_c(\mathbf{R}, \mathbf{C}) < E_c^*$ :
8:           $E_c^* := E_c(\mathbf{R}, \mathbf{C})$ 
9:           $\mathbf{R}^* := \mathbf{R}, \mathbf{C}^* := \mathbf{C}$ 
10: refine  $\mathbf{R}^*, \mathbf{C}^*$ 
```

c	... object index
E_c	... energy
τ	... inlier threshold
I	... set of image pixels
T	... set of regression trees

Sampling a Pose Hypothesis



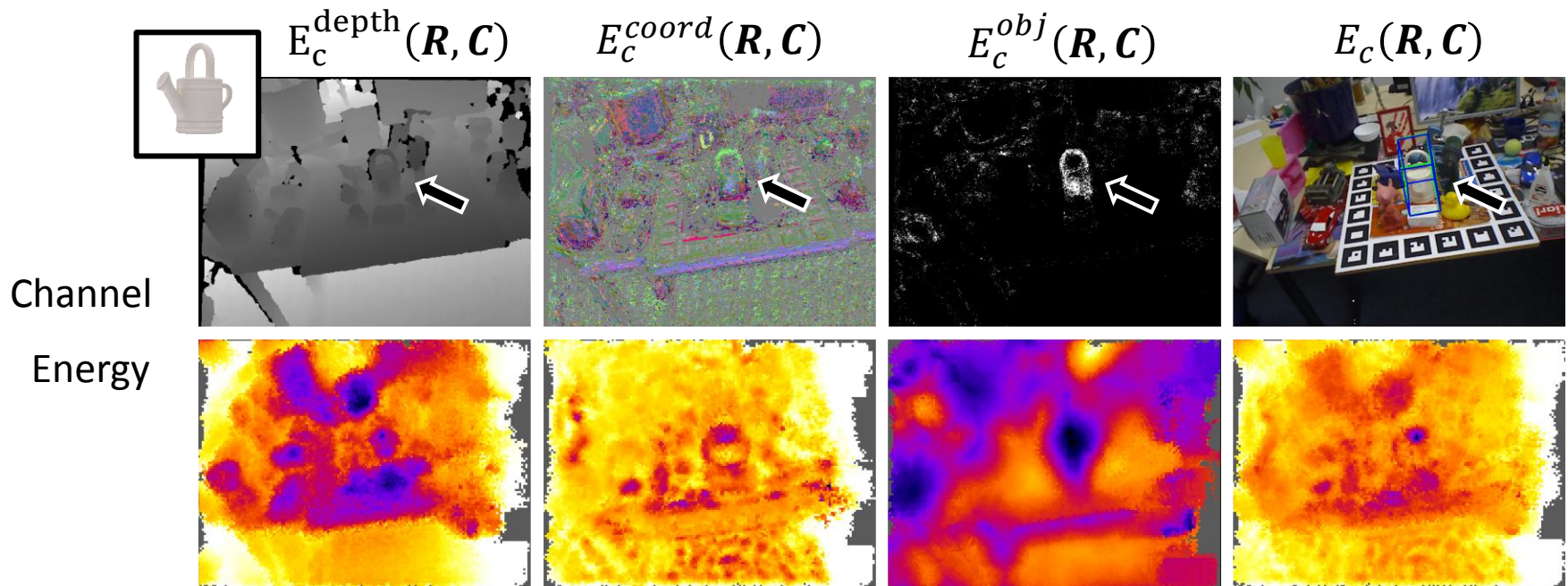
Energy Formulation

- Arbitrary 6DoF pose hypotheses $\mathbf{R}, \mathbf{C}$ is scored according to:

$$E_c(\mathbf{R}, \mathbf{C}) = \underbrace{\lambda^{\text{depth}} E_c^{\text{depth}}(\mathbf{R}, \mathbf{C})}_{\text{Comparison of depth}} + \underbrace{\lambda^{\text{coord}} E_c^{\text{coord}}(\mathbf{R}, \mathbf{C}) + \lambda^{\text{obj}} E_c^{\text{obj}}(\mathbf{R}, \mathbf{C})}_{\text{Comparison to forest prediction}}$$

Comparison of depth

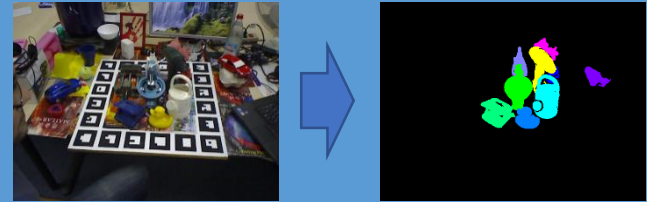
Comparison to forest prediction



Case Study: Pose Estimation and Pose Tracking

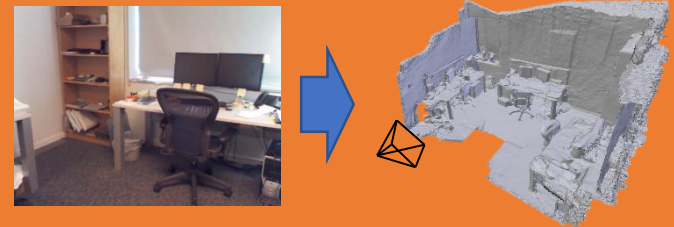
Image Segmentation:

- Decision Forest
- Features, Training Recap



Camera Re-Localization:

- Regression Forest
- Split-Criteria, Kabsch, RANSAC



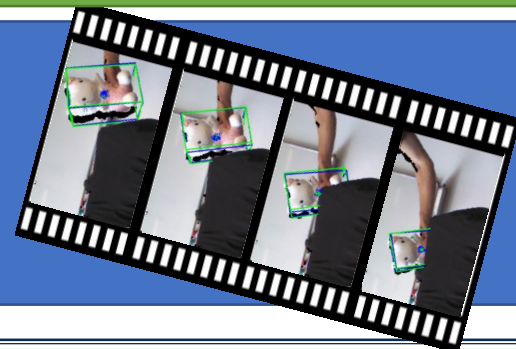
One-Shot Pose Estimation:

- Decision-Regression Forest
- Hypothesis Sampling, Hypotheses Energy



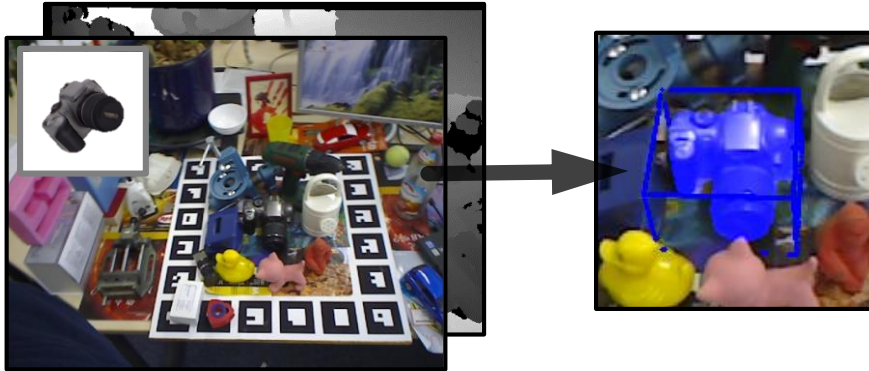
Object Pose Tracking

- Particle Filter
- Importance Sampling



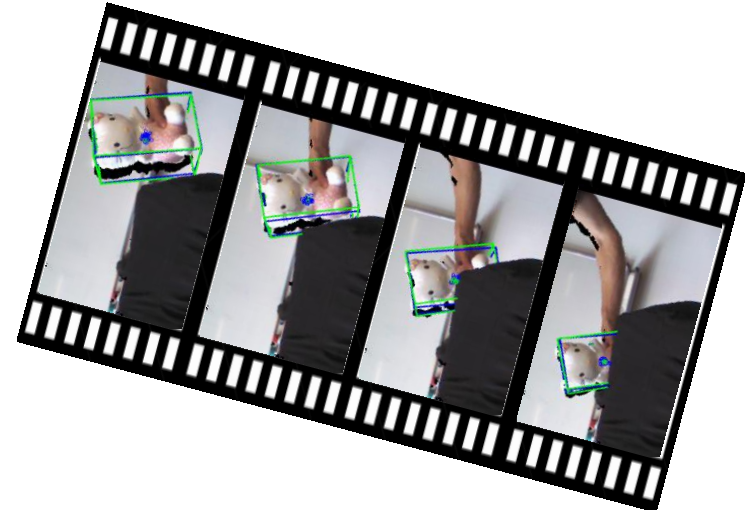
Pose Estimation vs. Pose Tracking

One Shot Pose Estimation [1]



- Estimate 6D Pose from **single** RGB-D image
- Use Object Coordinate Regression

Pose Tracking [2]



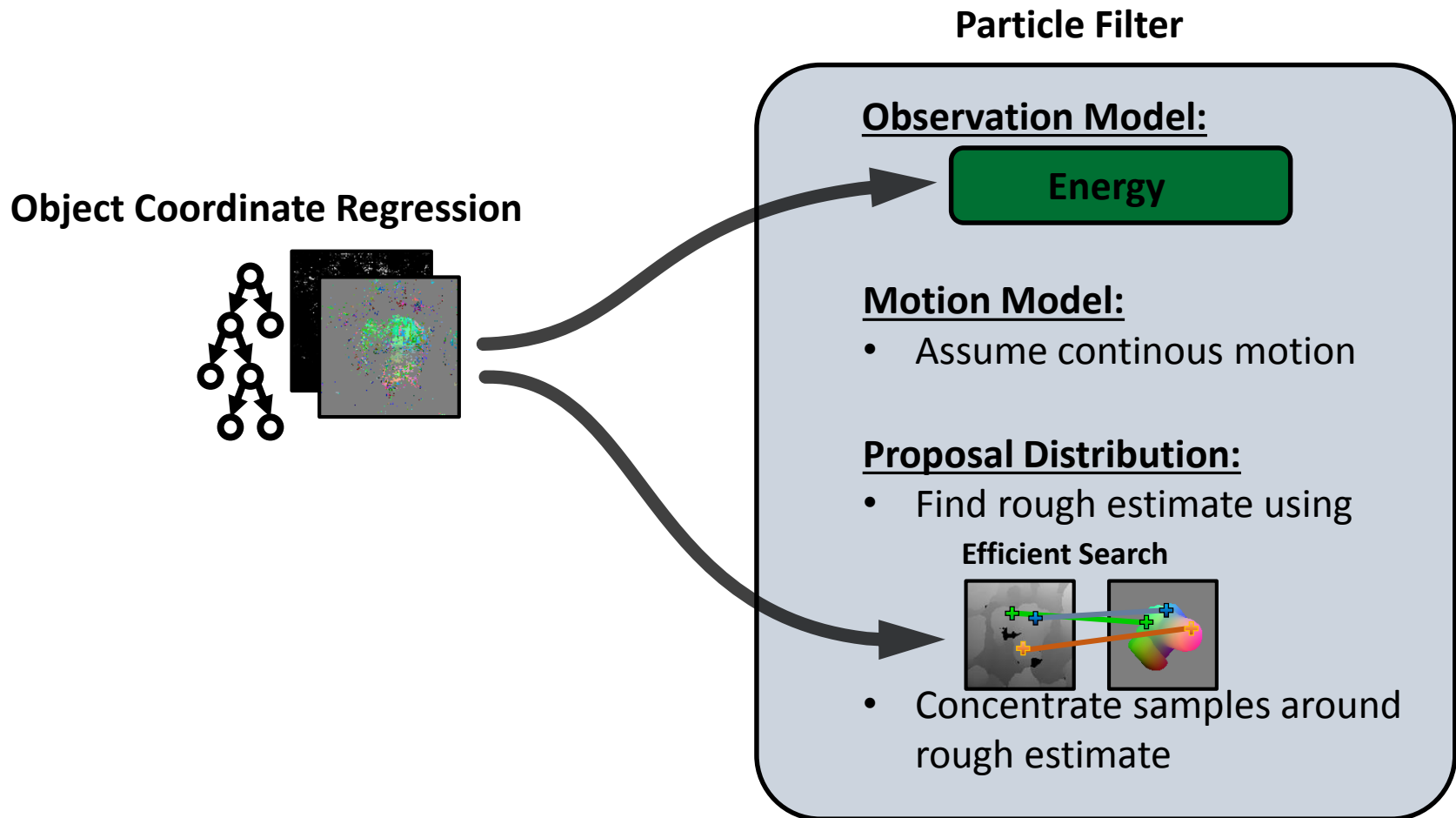
- **Stream** of RDB-D images
- Use information from previous frames:
 - Realtime
 - Increase robustness, accuracy

[1] Brachmann, E., Krull, A., Michel, F., Shotton, J., Gumhold, S., Rother, C.: Learning 6d object pose estimation using 3d object coordinates, ECCV (2014)

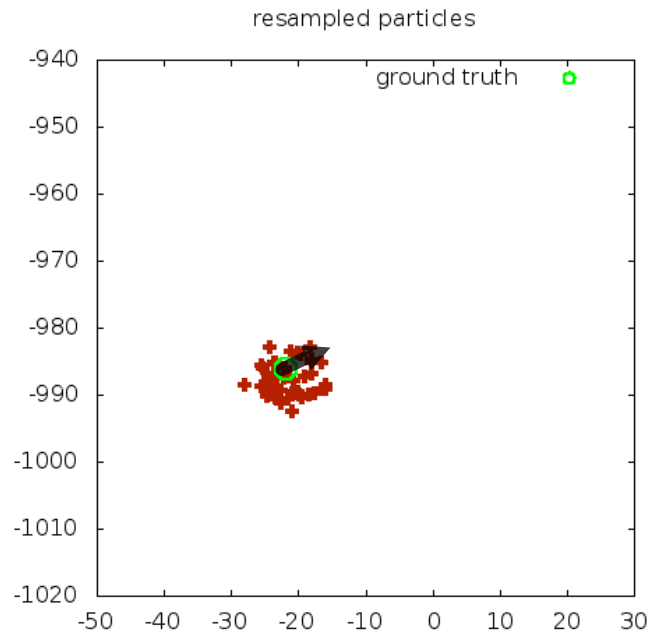
[2] Krull, A., Michel, F., Brachmann, E., Gumhold, S., Ihrke, S., Rother, C.: 6-DOF Model Based Tracking via Object Coordinate Regression, ACCV (2014)

How to Adapt it for Pose Tracking?

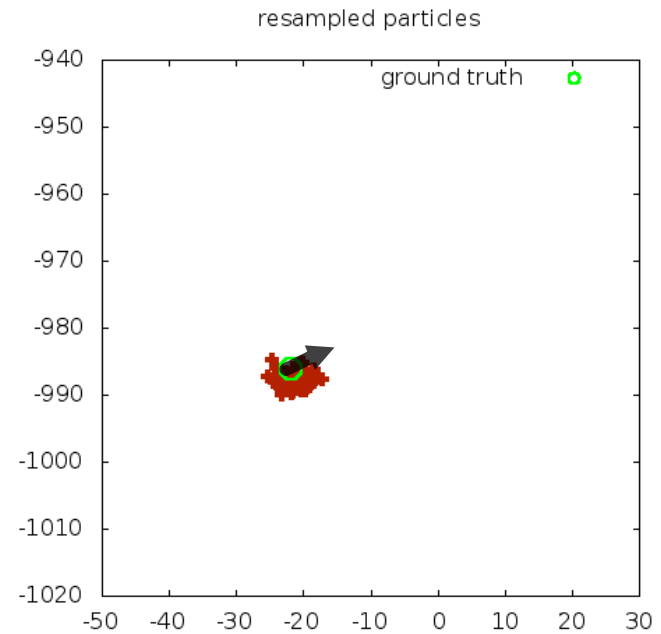
Ingredients:



Filtering with Object Coordinates

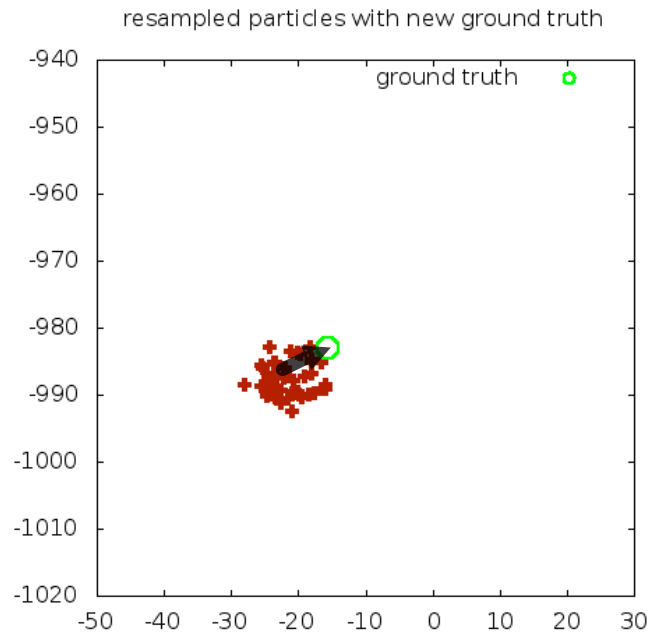


Sampling from Motion Model

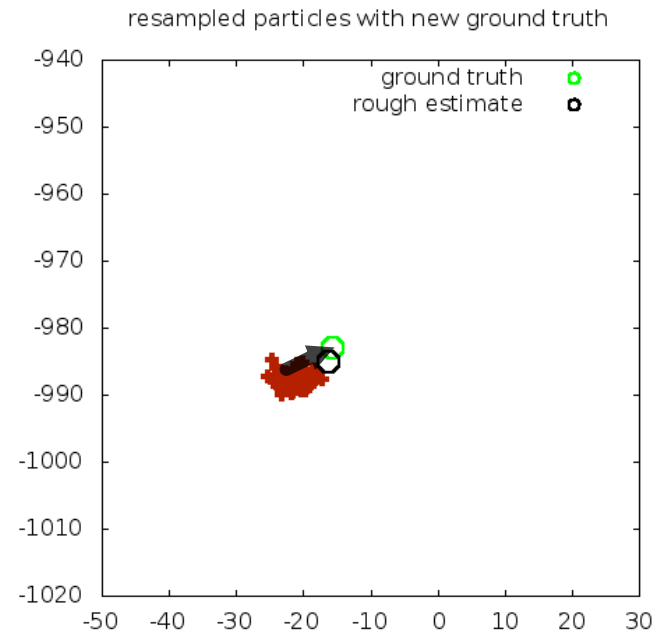


Sampling from Proposal Distribution

Filtering with Object Coordinates



Sampling from Motion Model

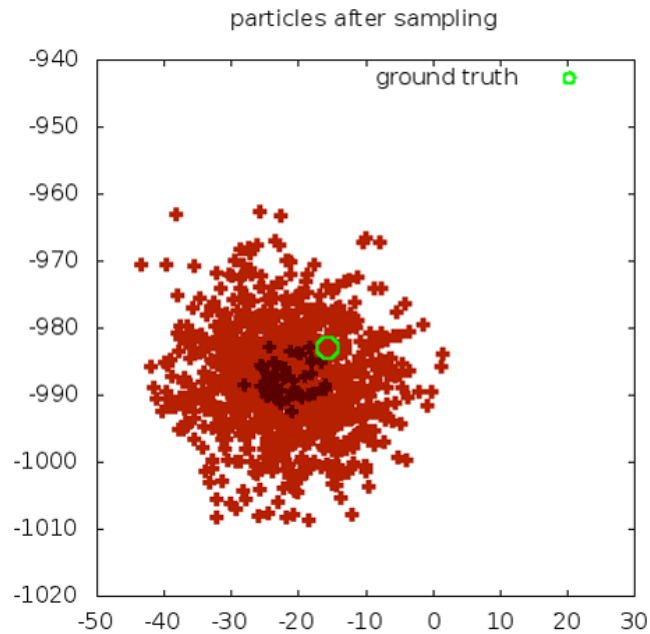


Sampling from Proposal Distribution

- Find a rough estimate for current pose

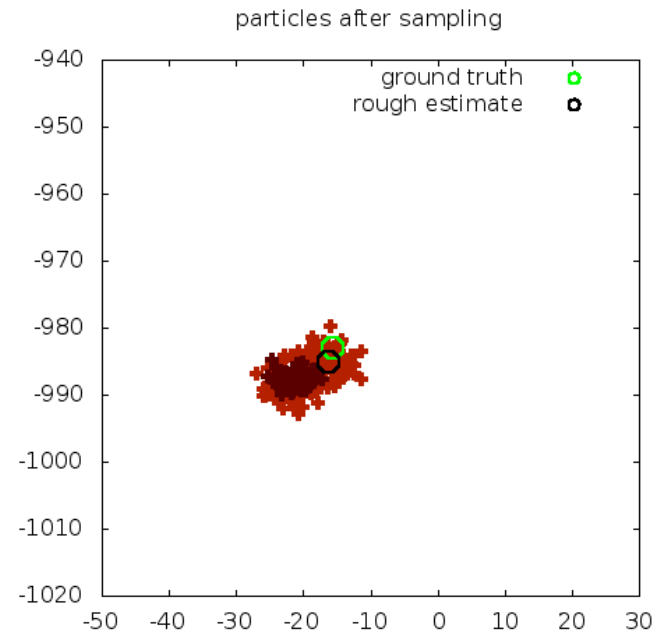


Filtering with Object Coordinates



Sampling from Motion Model

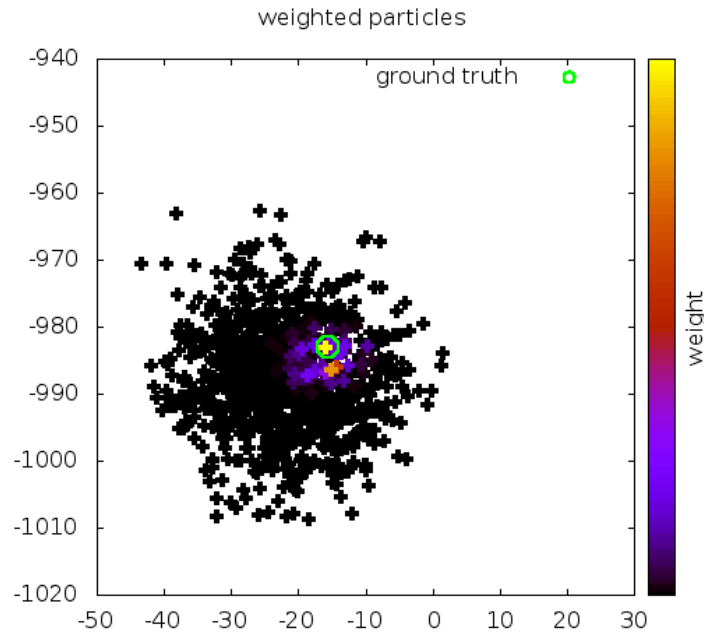
$$p(x_{t+1}|x_t)$$



Sampling from Proposal Distribution

$$q(x_{t+1}|x_t)$$

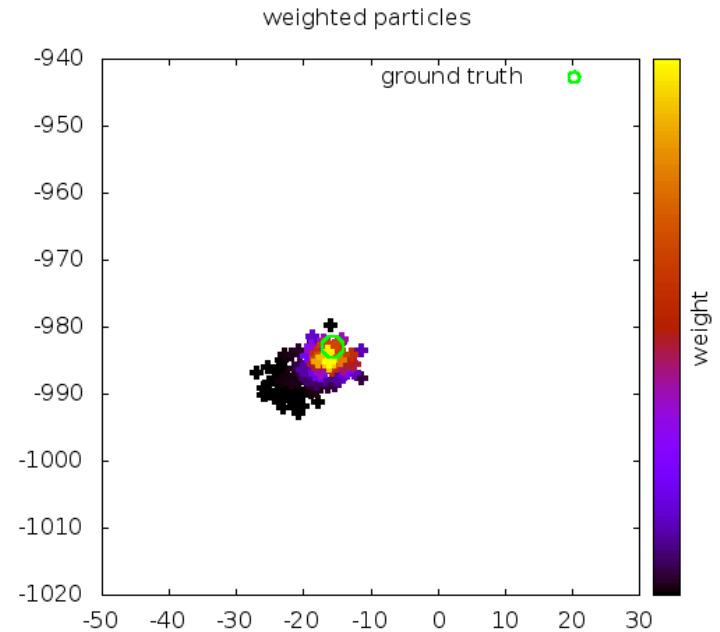
Filtering with Object Coordinates



Sampling from Motion Model

- Most samples have a very low weight

$$w_t^i = p(z_t | x_t = \tilde{x}_t^i)$$

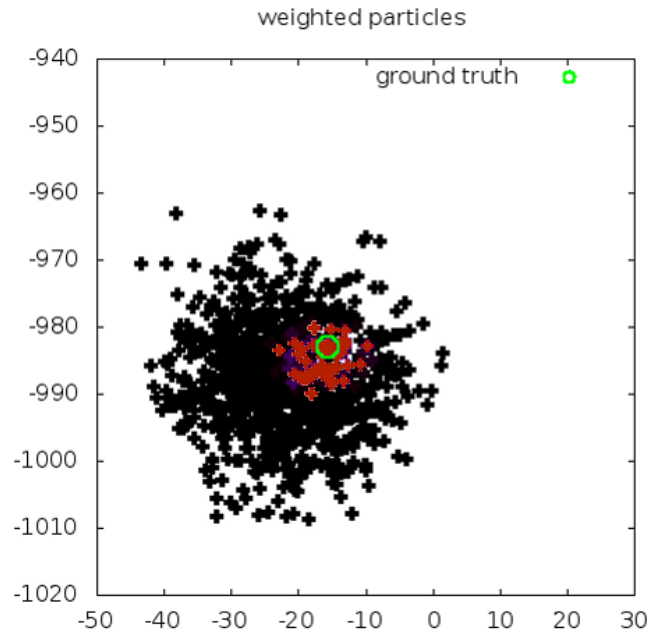


Sampling from Proposal Distribution

- Few samples have very low weight

$$w_t^i = p(z_t | x_t = \tilde{x}_t^i) \frac{p(x_t = \tilde{x}_t^i | x_{t-1} = \tilde{x}_{t-1}^i)}{q(x_t = \tilde{x}_t^i | x_{t-1} = \tilde{x}_{t-1}^i)}$$

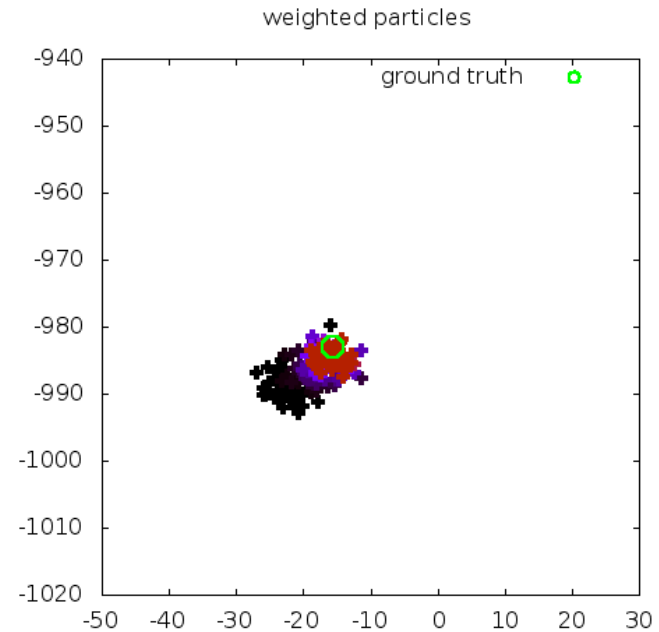
Filtering with Object Coordinates



Sampling from Motion Model

- Most samples have a very low weight

$$w_t^i = p(z_t | x_t = \tilde{x}_t^i)$$

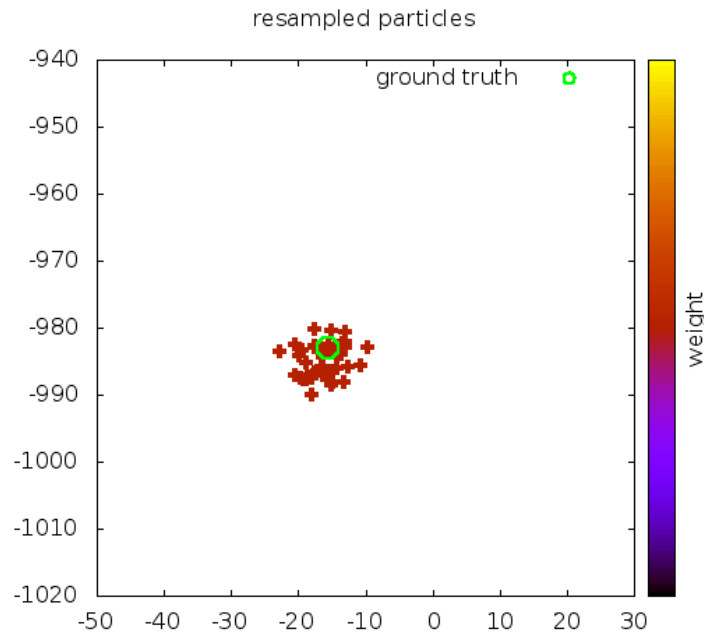


Sampling from Proposal Distribution

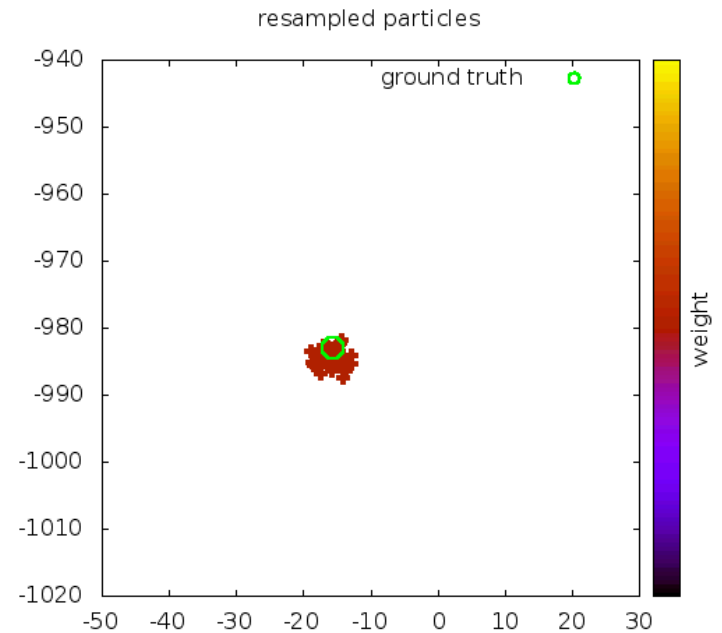
- Few samples have very low weight

$$w_t^i = p(z_t | x_t = \tilde{x}_t^i) \frac{p(x_{t+1} | x_t = \hat{x}_t^i)}{q(x_{t+1} | x_t = \hat{x}_t^i)}$$

Filtering with Object Coordinates



Sampling from Motion Model

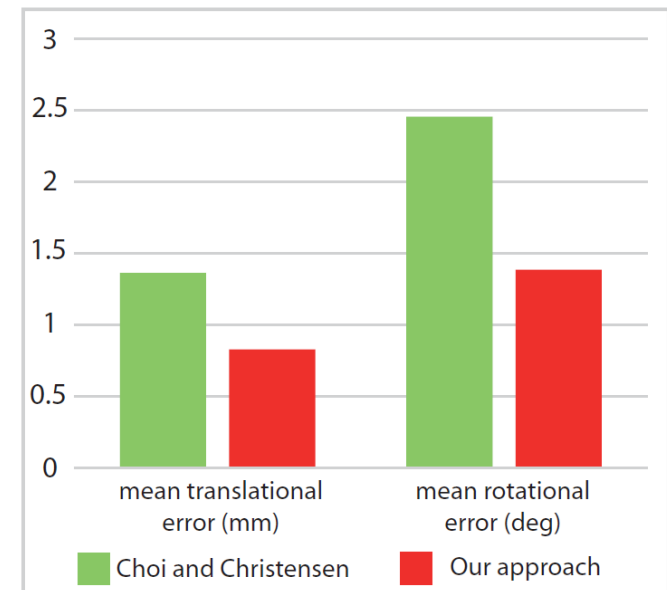


Sampling from Proposal Distribution

- More efficient
- Number of Particles can be reduced
- Frame rate can be increased

Evaluation: Choi and Christensen's Dataset [2]

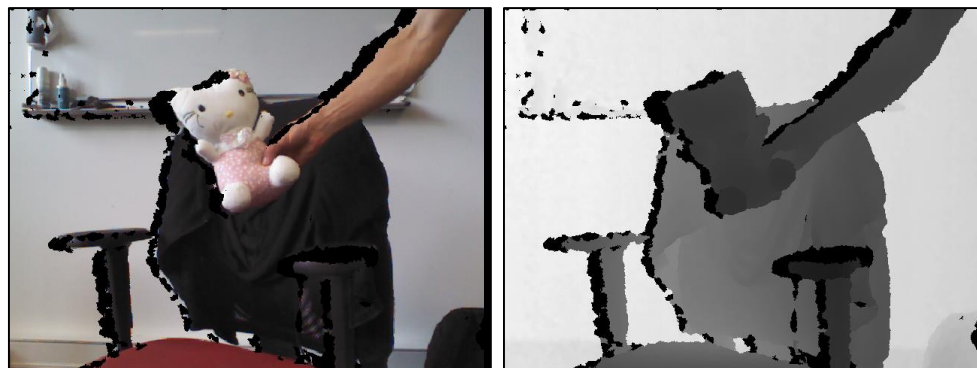
- A total of 4 synthetic sequences with 4 objects
- Objects placed in static environment
- Camera moving around object
- Partial occlusion
- Very exact ground truth



[2] Changyun Choi, Henrik I. Christensen, RGB-D Object Tracking: A Particle Filter Approach on GPU, IROS, 2013

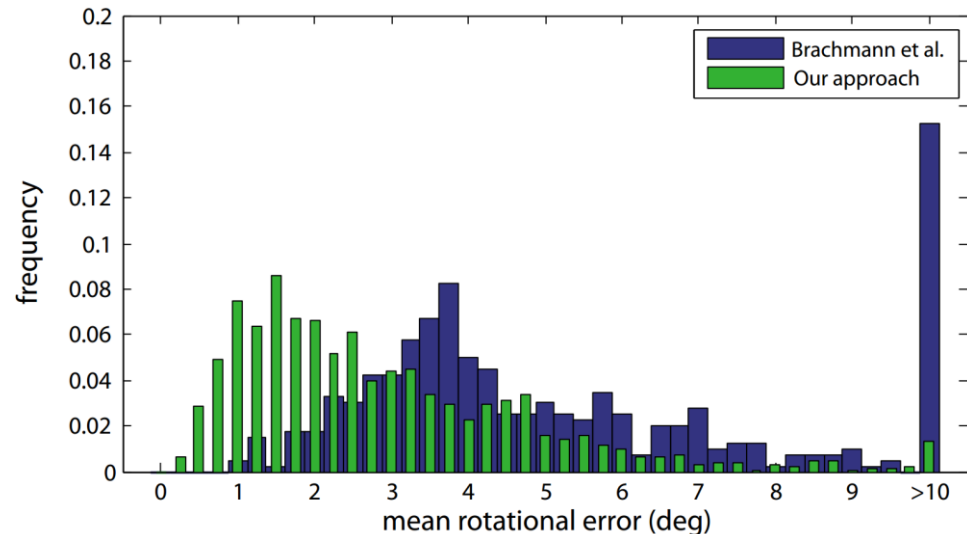
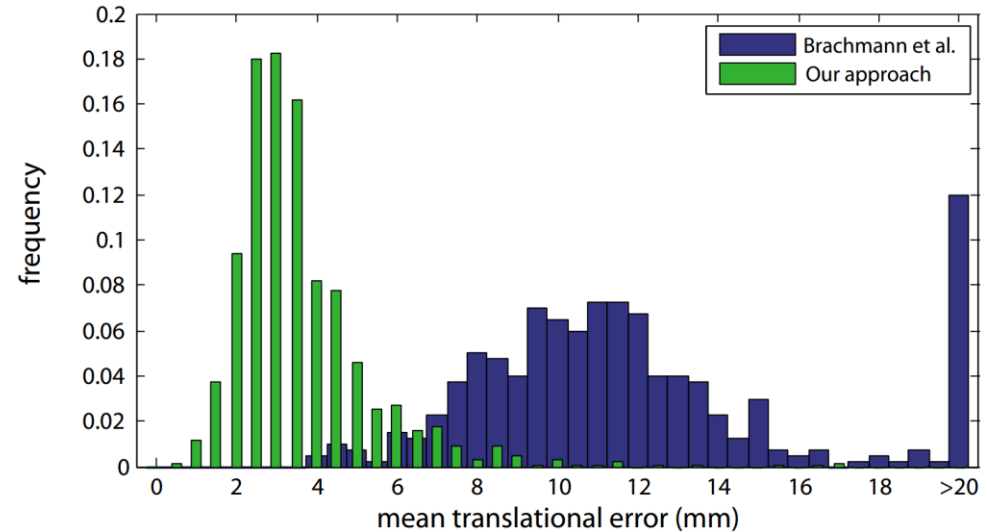
Evaluation: Our Dataset

- A total of 6 captured sequences of with 3 objects
- Manually annotated ground truth
- Moving objects in front of dynamic background
- Fast erratic movement
- Strong occlusions



Evaluation: Our Dataset

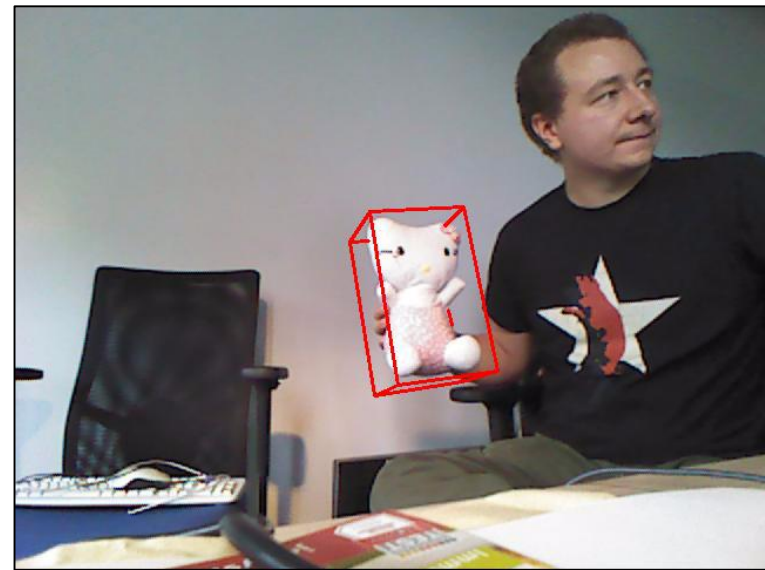
- Compared to [1] applied to each frame separately
- Lower average error
- Almost no outliers



Conclusion

- We have adapted the system from [1] for real time pose tracking
- We have designed a proposal distribution making efficient use of object coordinates
- Our method is robust against:
 - Quick motion
 - Strong occlusion
 - Shadows and changing light conditions
 - Deformation

[1] Brachmann, E., Krull, A., Michel, F., Shotton, J., Gumhold, S., Rother, C.: Learning 6d Object Pose Estimation Using 3d Object Coordinates, ECCV '14 (2014)



Recent Developments

- Articulated objects



- Learning the energy function

- Pose estimation from RGB

