





Objective

What:

• Fast and parallel algorithms for dense graphical models

Why:

- Dense graphical models are more expressive
- CNN+CRF training
- Huge datasets and Real Time Applications

MAP Inference



$$y^* = \underset{y \in \mathcal{Y}^{\mathcal{V}}}{\operatorname{arg\,min}} \left[E(y|\theta) := \sum_{v \in \mathcal{V}} \theta_v \right]$$

- • $\theta_v \rightarrow$ node potential.
- • $\theta_{uv} \rightarrow$ pairwise potential.
- $y^* \rightarrow$ optimal labelling.

Dual LP

To be able to deal with arbitrary potentials, we address the dual problem:

$$D(\phi) := \sum_{u \in \mathcal{V}} \min_{s \in \mathcal{Y}} \theta_u^{\phi}(s) + \sum_{uv \in \mathcal{E}} \min_{(s,t) \in \mathcal{Y}^2} \theta_{uv}^{\phi}(s,t) .$$
(1)
$$\theta_u^{\phi}(s) := \theta_u(s) + \sum_{v \in \mathrm{Nb}(u)} \phi_{v \to u}(s)$$

$$\theta_{uv}^{\phi}(s,t) := \theta_{uv}(s,t) - \phi_{v \to u}(s) - \phi_{u \to v}(t) .$$

Dual variables $\phi_{u \to v}$ and $\phi_{v \to u}$ are the Lagrange multipliers.



 $D(\phi)$ is

- concave
- piece-wise linear
- non-smooth

MPLP++: Fast, Parallel Dual Block-Coordinate Ascent (BCA) for Dense Graphical Models Siddharth Tourani¹ Alexander Shekhovtsov ² Carsten Rother¹ Bogdan Savchynskyy¹ Visual Learning Lab, IWR, University of Heidelberg, Germany Centre for Machine Perception, Czech Technical University,

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Motivation for Algorithm Structure

- The subgradient for the dual is sparse. Block Coordinate Ascent methods are more efficient than sub-gradient based methods.
- TRWS [1] is the best performer for MAP inference.
- Dense graphs need no large sub-problem decompositions.

Comparing BCA Updates

$$g_{uv}(s,t) = \theta_{uv}(s,t) + \theta_u(s) + \theta_v(t)$$

$$\begin{array}{c}
0 \\
0 \\
0 \\
u \\
u \\
Initial
\end{array}$$

3.5



MPLP: [2]

MPLP++:

 $\theta_u^{\mathcal{M}}(s) := \frac{1}{2} \min_{t \in \mathcal{Y}} g_{uv}(s)$ $\theta_v^{\mathcal{M}}(t) := \frac{1}{2} \min_{s \in \mathcal{Y}} g_{uv}(t)$

$$2$$

$$3.5$$

$$u$$

$$u$$

$$MPLP$$

$$2$$

$$2$$

$$2$$

$$2$$

$$2$$

$$3.5$$

We prove

Parallelization: CPU & GPU



Non-incident edges can be processed in parallel. \rightarrow We use maximum matching solvers.



$$u = \frac{0}{1.5}$$

$$s, t), \ \forall s \in \mathcal{Y},$$
 (\mathcal{M})
$$s, t), \ \forall t \in \mathcal{Y}.$$

$$2 \underbrace{0}_{0} \underbrace{0}_{1} \underbrace{0}_{1}$$

$$\begin{aligned} \theta_{u}^{\mathcal{H}}(s) &:= \theta_{u}^{\mathcal{M}}(s), \quad \theta_{v}^{\mathcal{H}}(s) := \theta_{v}^{\mathcal{M}}(s), \, \forall s \in \mathcal{Y}, \\ \theta_{v}^{\mathcal{H}}(t) &:= \theta_{v}^{\mathcal{H}}(t) + \min_{s \in \mathcal{Y}} [g_{uv}(s,t) - \theta_{v}^{\mathcal{H}}(t) - \theta_{u}^{\mathcal{H}}(s)], \, \forall t \in \mathcal{Y}, \quad (\mathcal{H}) \\ \theta_{u}^{\mathcal{H}}(s) &:= \theta_{u}^{\mathcal{H}}(s) + \min_{t \in \mathcal{Y}} [g_{uv}(s,t) - \theta_{v}^{\mathcal{H}}(t) - \theta_{u}^{\mathcal{H}}(s)], \, \forall s \in \mathcal{Y}. \end{aligned}$$

With same input, at the end of the first iteration, $D(\phi^{\mathcal{M}}) \leq D(\phi^{\mathcal{H}})$.



(e) protein (100% density, 40 vars, up to 200 states)



(**g**) pose (100% density, 600-4800 nodes, 13 states)



Conclusions and Outlook

- tion, CVWW 2016.



This project has received funding from the ERC under the European Unions Horizon 2020 research and innovation program (grant agreement No 647769). A. Shekhovtsov was supported by Czech Science Foundation grant 18-25383S.



Results





(f) worms (10% density, 556 vars, 40-50 states)



(h) stereo (tsukuba, venus, teddy, grid graph, 12-60 states)

Figure 1: Dual versus time



Figure 2: Obtained Speedups

• Our approach is the state-of-the-art method for dense graphical models (> 10% graph density), beating even TRWS. • We give CPU and GPU parallel implementations provided at https://gitlab.com:tourani.siddharth/mplpplusplus.git.

References

[1] Kolmogorov, V., "Convergent tree-reweighted message passing for energy minimization", PAMI, 2006. [2] Globerson et al., "Fixing Max-Product: Convergent Message Passing Algorithms for MAP LP-Relaxations", NIPS, 2008. [3] A. Shekhovtsov, C. Reinbacher, G.Graber and T. Pock: Solving Dense Image Matching in Real-Time Using Discrete-Continuous Optimiza-

Acknowledgements