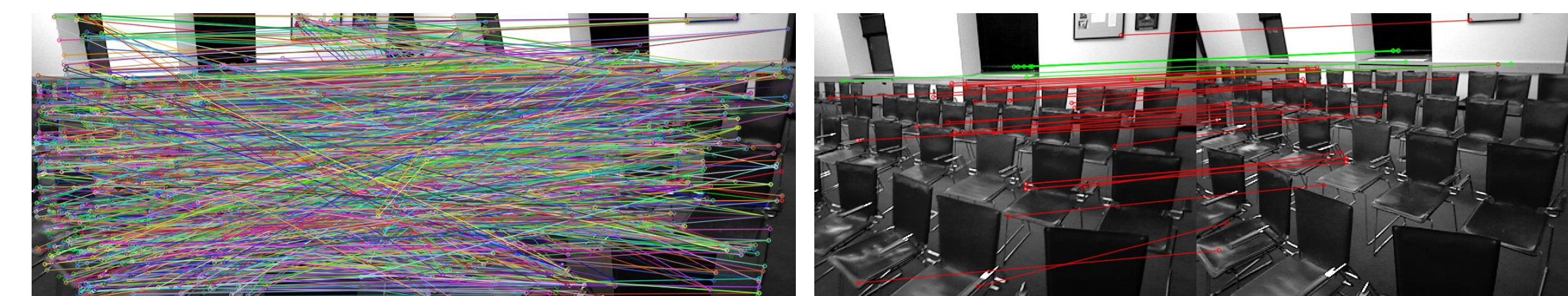




Problem Statement

Fit a parametric model to data points with **many outliers** using RANSAC.

For example, fit essential matrix to SIFT correspondences.



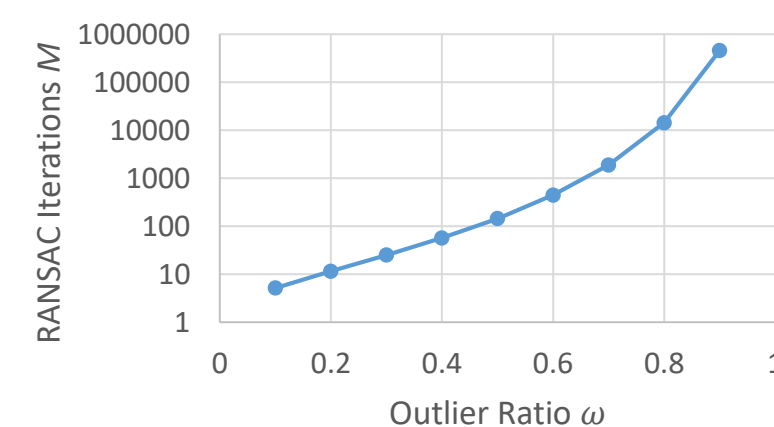
2000 SIFT correspondences, outlier ratio: 88%
RANSAC would need: > 185.000 iterations

Result after 1000 iterations (OpenCV)

Number of RANSAC iterations grows exponentially with increasing outlier ratio.

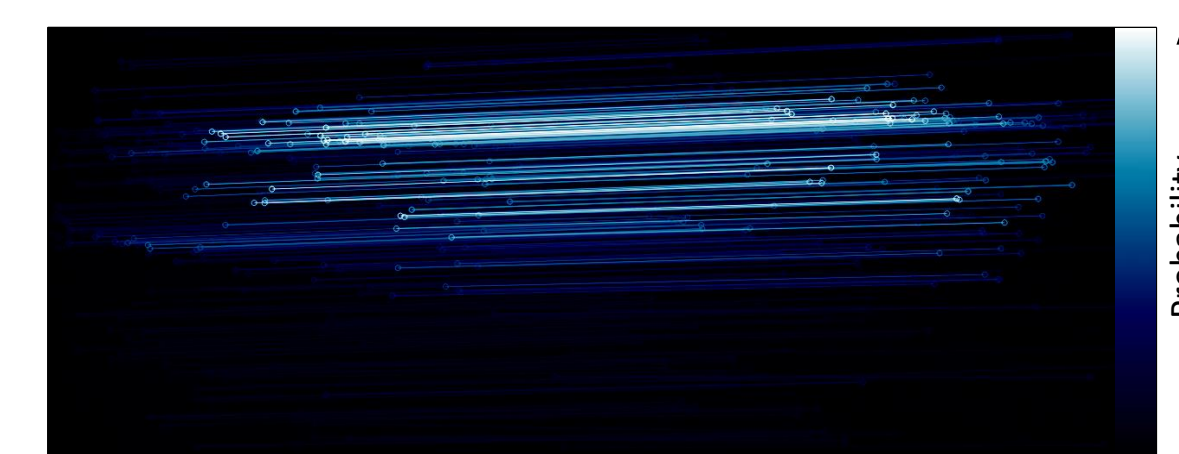
$$M = \frac{\log(1-p)}{\log(1-(1-\omega)^n)}$$

Target probability: $p = 0.99$
Minimal set size: $n = 5$

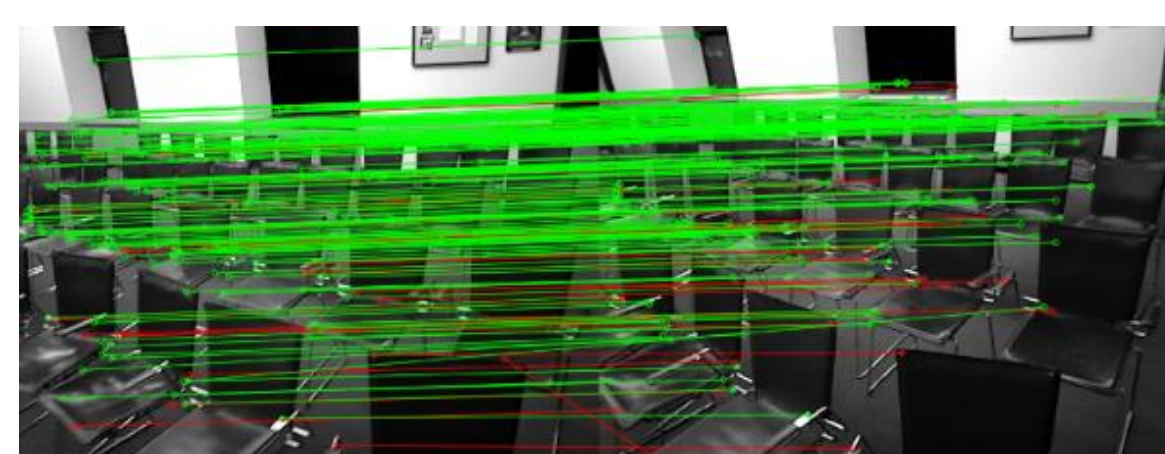


→ Removing **just enough** outliers makes the problem **exponentially easier**.

→ We let a **neural network** predict weights that **guide RANSAC** sampling.



239 correspondences get 90% probability mass,
outlier ratio: 33%



NG-RANSAC result after 1000 iterations

Contributions

- NG-RANSAC: A **general, robust estimator** based on RANSAC with learned guidance of hypotheses sampling
- Principled learning formulation that directly **optimizes model quality**
- Training with **non-differentiable** minimal solver, refinement, loss etc., also training **self-supervised** sampling
- Applied to estimation of **essential matrices, fundamental matrices, horizon lines, and camera poses**

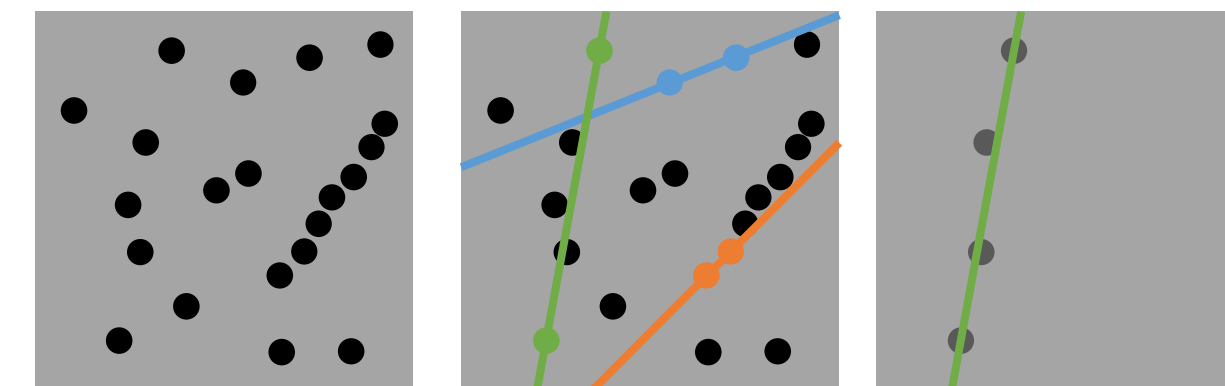
Background: RANSAC

1) Sampling Hypotheses:

$$p(\mathbf{h}) = \prod_{i=0}^N p(y_i) \text{ with } p(y) = \frac{1}{|Y|}$$

uniform weights

$$p(\mathcal{H}) = \prod_{j=0}^M p(\mathbf{h}_j)$$



data points $y \in Y$ hypotheses $\mathbf{h} \in \mathcal{H}$ fitted model $\hat{\mathbf{h}}$

2) Hypothesis Selection:

$$\hat{\mathbf{h}} = \operatorname{argmax}_{\mathbf{h} \in \mathcal{H}} s(\mathbf{h}, Y)$$

$$s(\mathbf{h}, Y) = \sum_{y \in Y} \mathbb{1}[d(y, \mathbf{h}) < \tau]$$

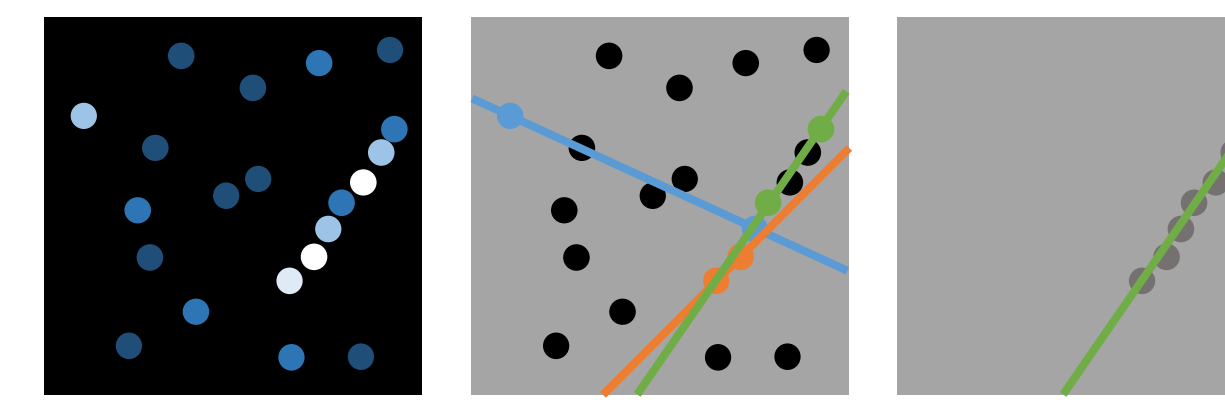
inlier count:

Neural-Guided RANSAC

Guided Sampling:

$$p(\mathbf{h}) = \prod_{i=0}^n p(y_i) \text{ with } p(y) = g(Y; \mathbf{w})$$

learned weights



neural guidance $g(Y; \mathbf{w})$ hypotheses $\mathbf{h} \in \mathcal{H}$ fitted model $\hat{\mathbf{h}}$

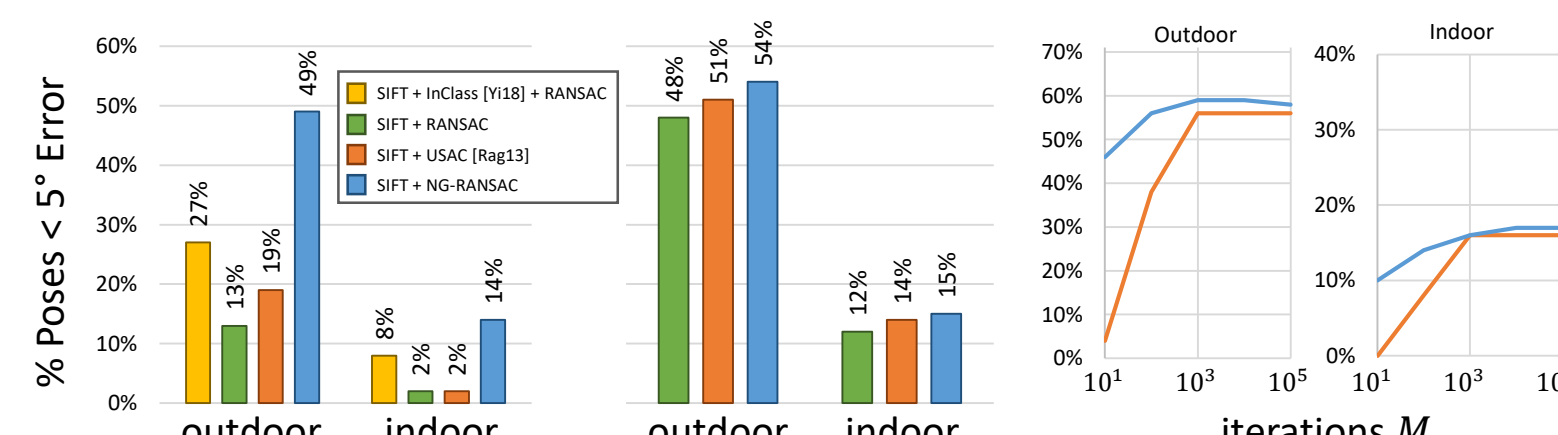
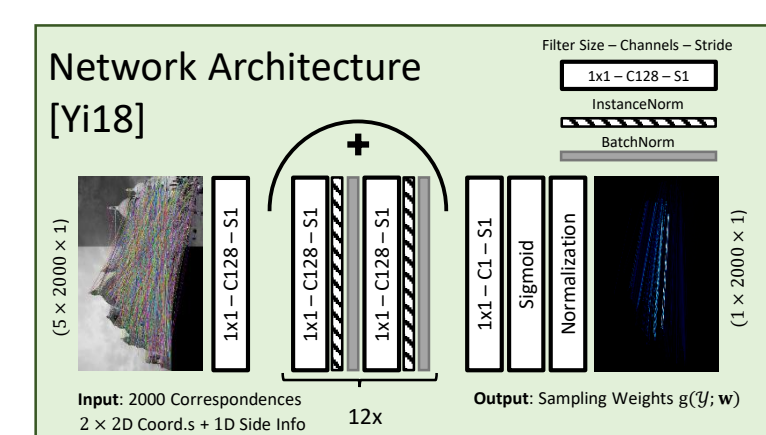
Training Objective:

$$\frac{\partial}{\partial \mathbf{w}} \mathbb{E}_{\mathcal{H} \sim p(\mathcal{H}; \mathbf{w})} [\ell(\hat{\mathbf{h}})] = \mathbb{E}_{\mathcal{H} \sim p(\mathcal{H}; \mathbf{w})} \left[\ell(\hat{\mathbf{h}}) \frac{\partial}{\partial \mathbf{w}} \log p(\mathcal{H}; \mathbf{w}) \right] \approx \frac{1}{K} \sum_{k=1}^K \left[\ell(\hat{\mathbf{h}}) \frac{\partial}{\partial \mathbf{w}} \log p(\mathcal{H}_k; \mathbf{w}) \right]$$

expected loss gradients approximate via sampling

Application: Epipolar Geometry

Essential matrix from SIFT correspondences: without side information with side information and Lowe's ratio filter



Fundamental matrix from SIFT correspondences:

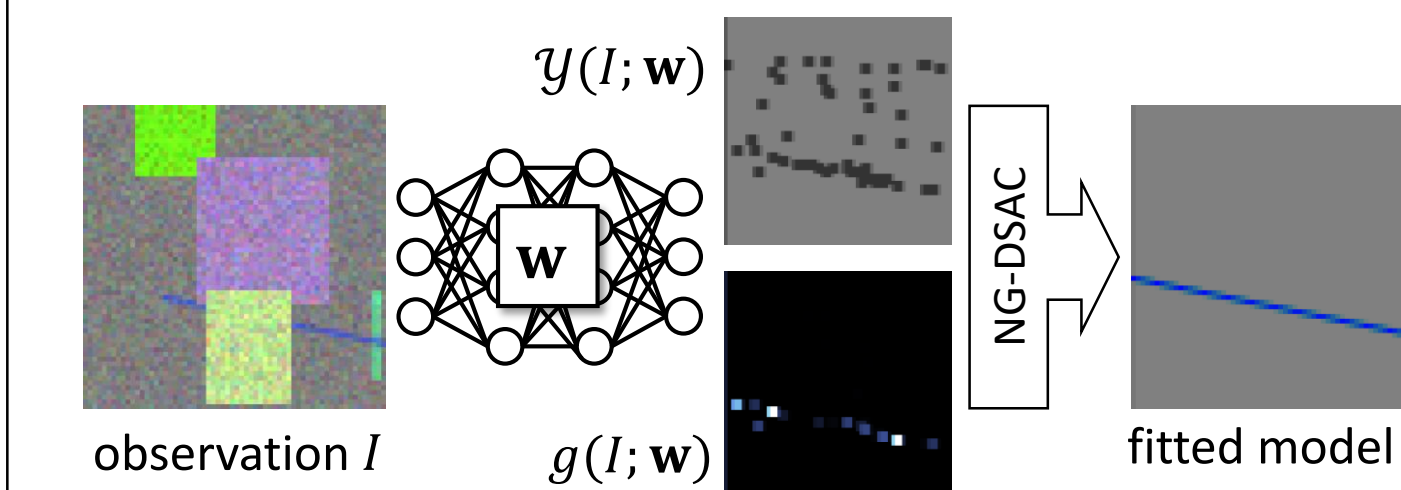


	Training Objective	% Inliers	F-score	Mean	Median
RANSAC	-	21.85	13.84	0.35	0.32
USAC [Rag13]	-	21.43	13.90	0.35	0.32
Deep F-Mat [Ran18]	Mean	24.61	14.65	0.32	0.29
NG-RANSAC	Mean	25.05	14.76	0.32	0.29
NG-RANSAC	F-score	24.13	14.72	0.33	0.31
NG-RANSAC	%Inliers	25.12	14.74	0.32	0.29

$\ell(\hat{\mathbf{h}}) = -s(\hat{\mathbf{h}}, Y)$
Self-Supervised!

Neural-Guided DSAC

Let a network **predict** not only **sampling weights** but **data points** themselves.



Background: DSAC [Bra17]

$$\hat{\mathbf{h}} = \mathbf{h}_j \text{ with } j \sim p(j) = \frac{\exp(s(\mathbf{h}_j, Y))}{\sum_{j'} \exp(s(\mathbf{h}_{j'}, Y))}$$

Training Objective

$$\mathcal{L}(\mathbf{w}) = \mathbb{E}_{j \sim p(j)} [\ell(\mathbf{h}_j)]$$

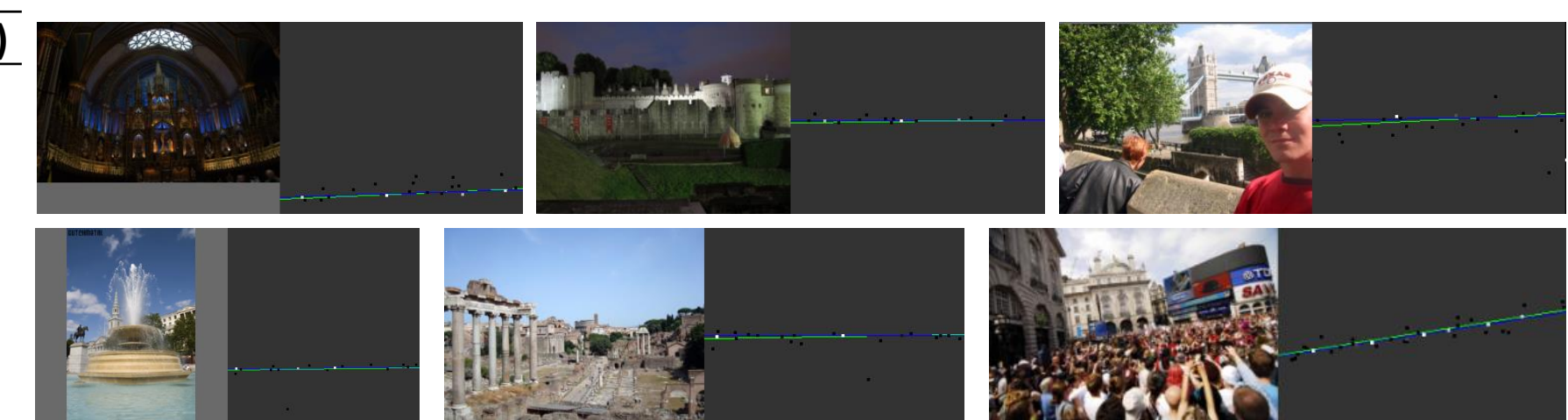
NG-DSAC Training Objective:

$$\frac{\partial}{\partial \mathbf{w}} \mathbb{E}_{\mathcal{H} \sim p(\mathcal{H}; \mathbf{w})} \mathbb{E}_{j \sim p(j|\mathcal{H})} [\ell(\mathbf{h}_j)] \approx \frac{1}{K} \sum_{k=1}^K \left[\mathbb{E}_j [\ell] \frac{\partial}{\partial \mathbf{w}} \log p(\mathcal{H}_k; \mathbf{w}) + \mathbb{E}_j [\ell] \right]$$

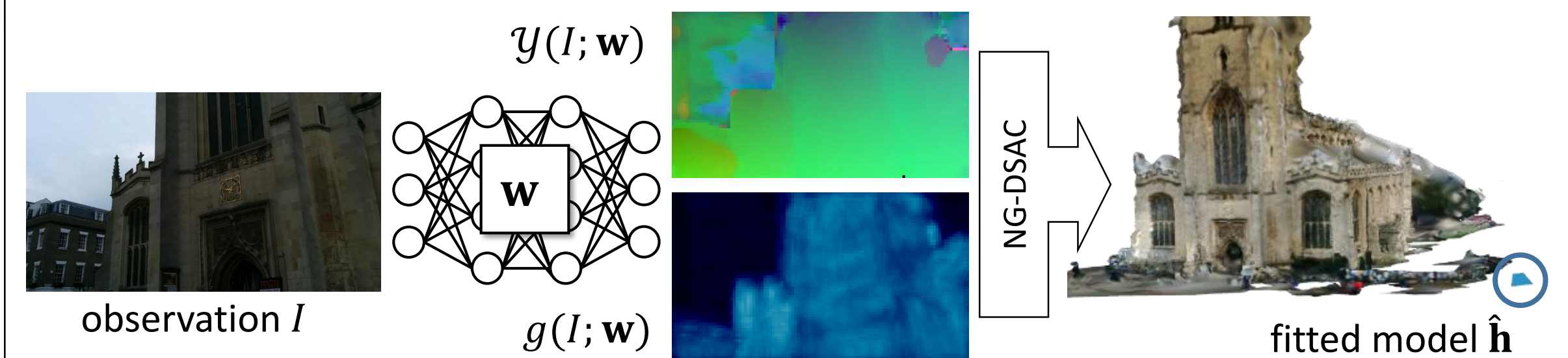
expected loss approximated gradients

Application: Horizon Line Estimation

on [Wor16]	AUC (%)
Simon et al.	54.4
Kluger et al.	57.3
Zhai et al.	58.2
Workman et al.	71.2
DSAC	74.1
NG-DSAC	75.2
SLNet	82.3



Application: Camera Re-Localization



on [Ken15]	PoseNet	Active Search	DSAC++ [Bra18]	NG-DSAC++
Great Court	700cm	-	40.3cm	35.0cm
Kings College	99cm	42cm	13.0cm	12.6cm
Old Hospital	217cm	44cm	22.4cm	21.9cm
Shop Facade	107cm	12cm	5.7cm	5.6cm
St M. Church	149cm	19cm	9.9cm	9.8cm

